



## Introduction to Doppler Cloud Radar

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*CCRES/CLU Training school, Munich, 2-5 Sept. 2025*

# Outline

## Introduction

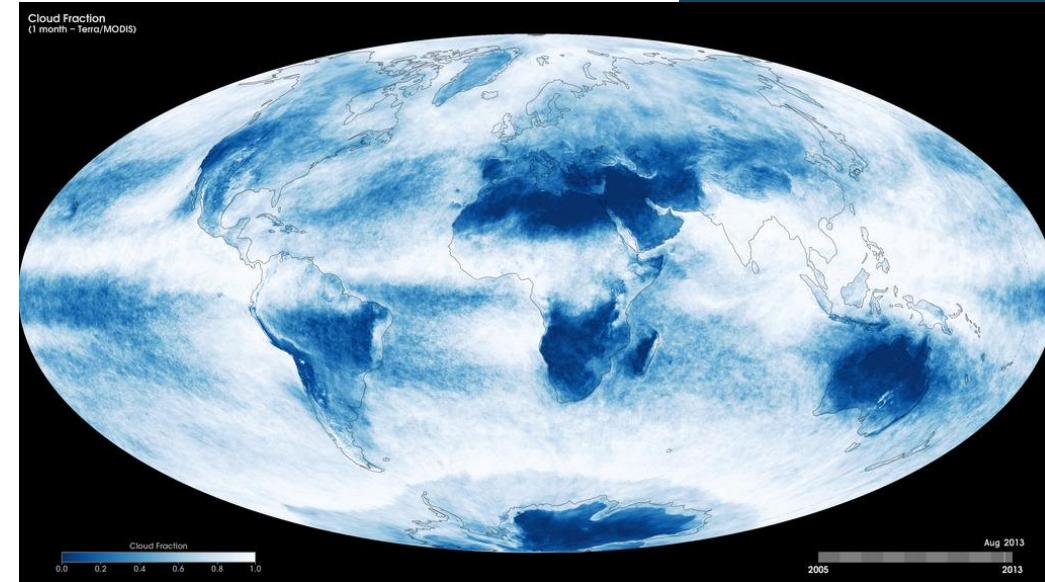
1. **Radar principles & cloud radars**
2. **Radar equation (Power)**
3. **Doppler velocity (Phase)**
4. **From DSD to Moments**
5. **Doppler Spectra**
6. **Polarimetry**

## References

# Introduction: why observe Clouds ?

## Clouds: a key Climate regulator

- **Clouds cover** about  $\frac{2}{3}$  of Earth's surface and play a **complex** role in the **climate system**
- They **both cool and warm the planet**, but the **net effect** depends on their **type, altitude, and structure**
  - **Low clouds** (e.g. stratus) are typically thick, extensive and reflective → they tend to **cool** the planet by reflecting incoming solar radiation ("parasol" effect)
  - **High clouds** (e.g. cirrus) are cold and thin, letting solar radiation in but trapping outgoing longwave radiation → they tend to **warm** the planet
  - **On average, clouds** have a **net cooling effect on Earth** (mainly due to low clouds)

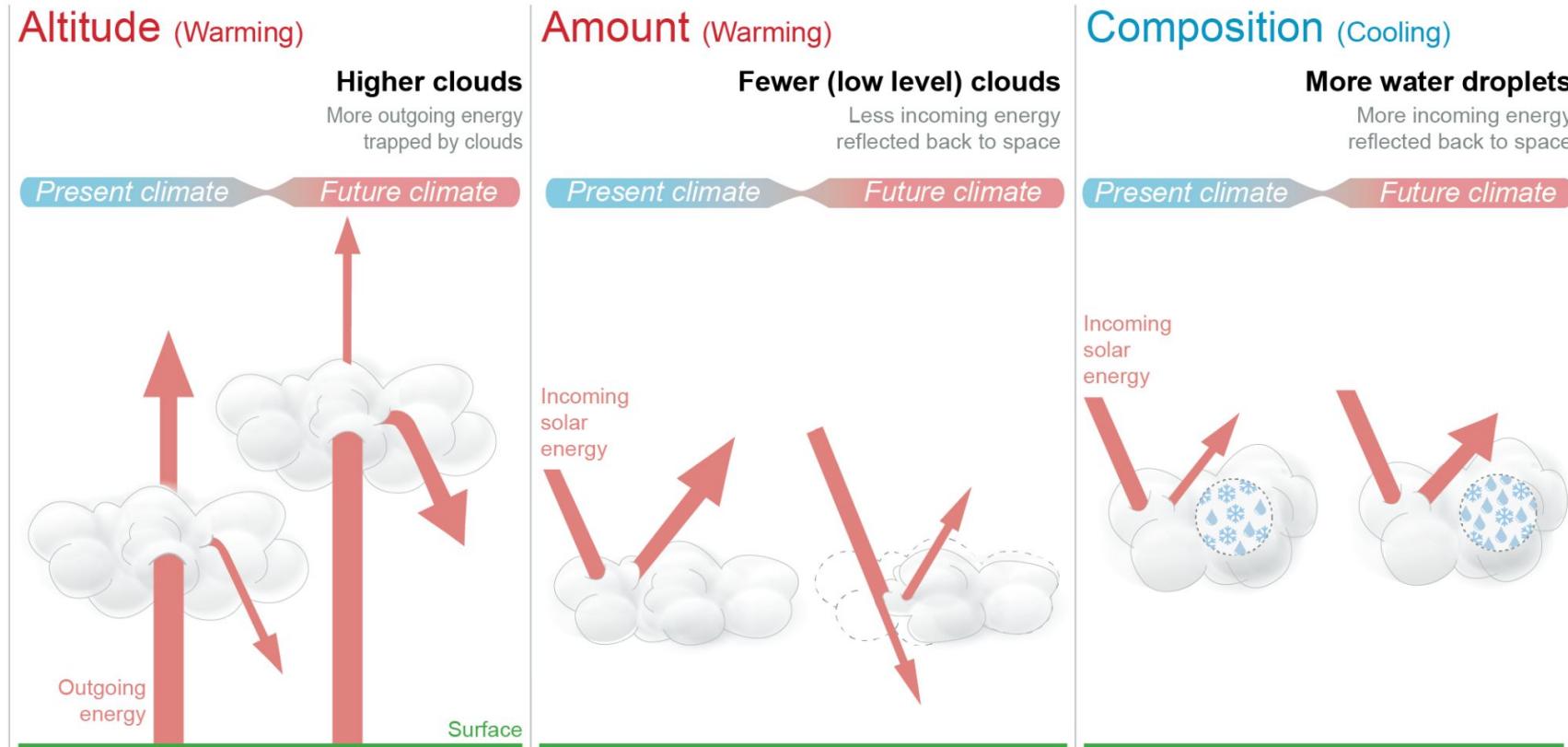


<https://earthobservatory.nasa.gov/>

# Introduction: why observe Clouds ?

## FAQ 7.2: What is the role of clouds in a warming climate?

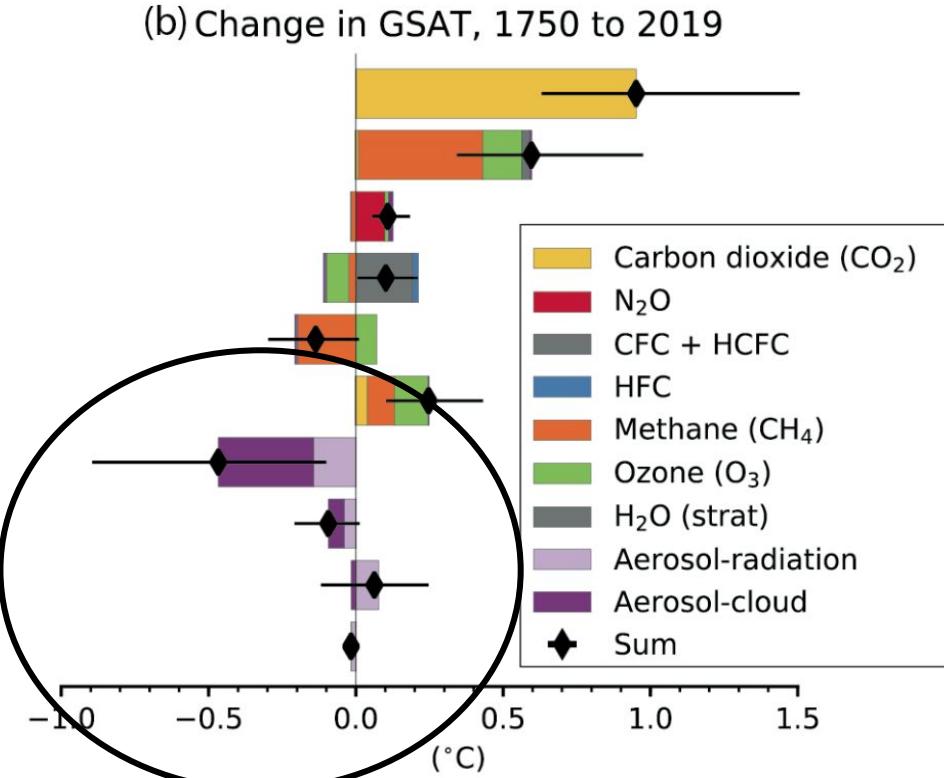
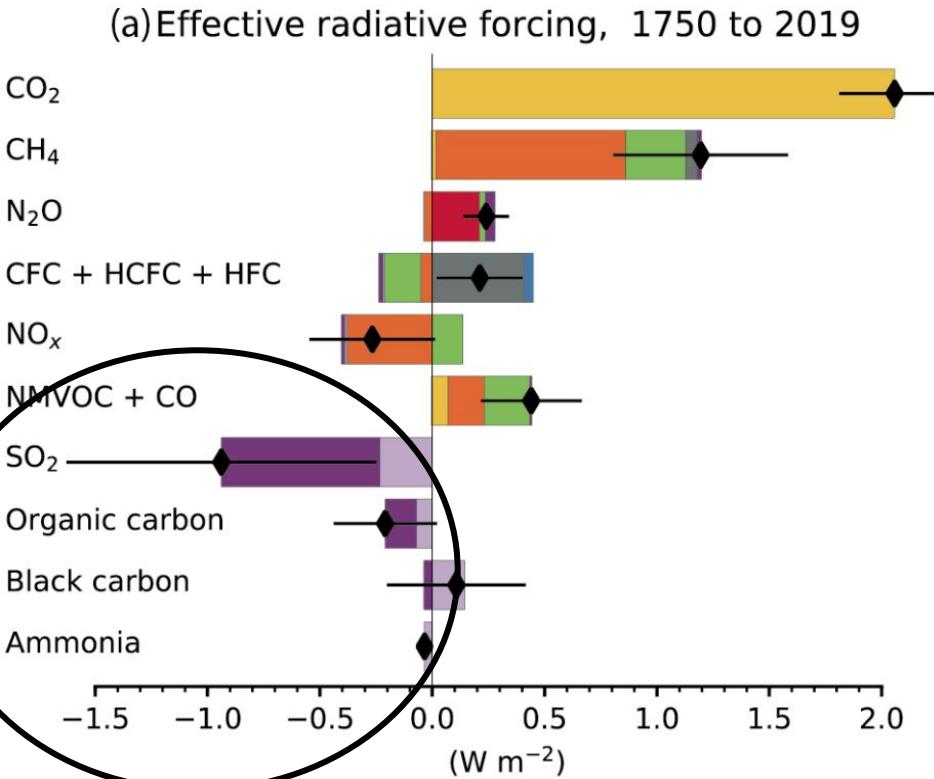
Clouds affect and are affected by climate change. Overall, scientists expect clouds to **amplify future warming**.



IPCC, 2021 – FAQ 7.2 Fig. 1, AR6 WG1, Chap. 7: Earth's Energy Budget, Climate Feedbacks, and Climate Sensitivity. DOI: <https://doi.org/10.1017/9781009157896.009>

# Introduction: why observe Clouds ?

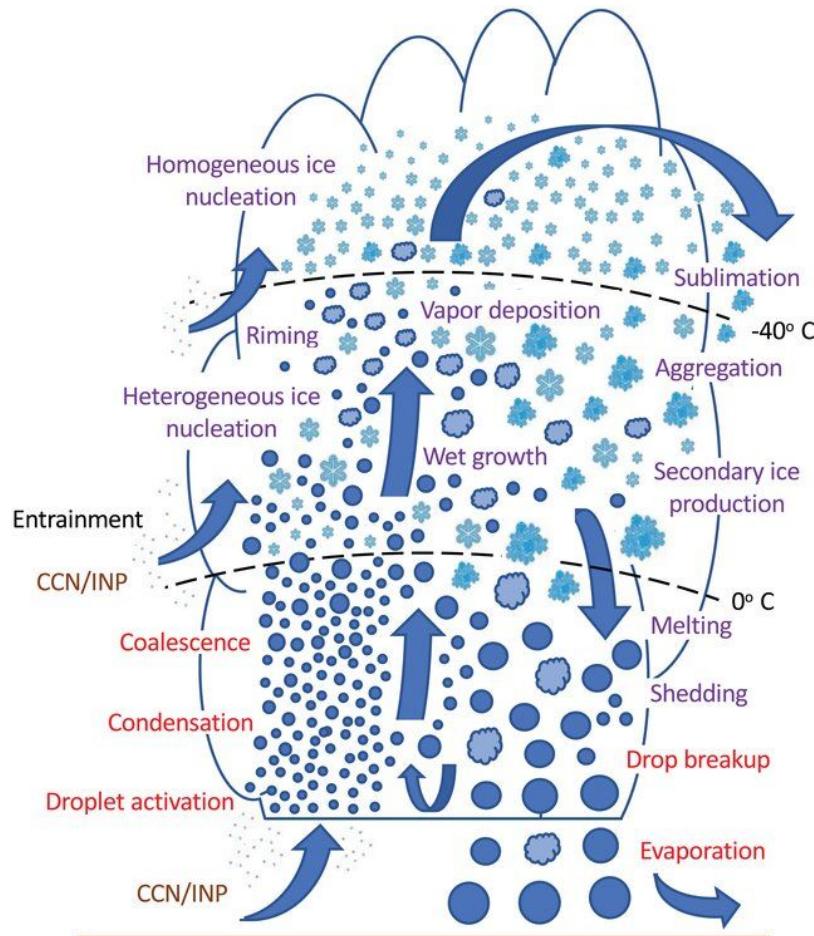
Cooling wins → but **large** associated **uncertainties**



From Figure 6.12 in IPCC, 2021: Chapter 6, DOI:  
<https://doi.org/10.1017/9781009157896.008>

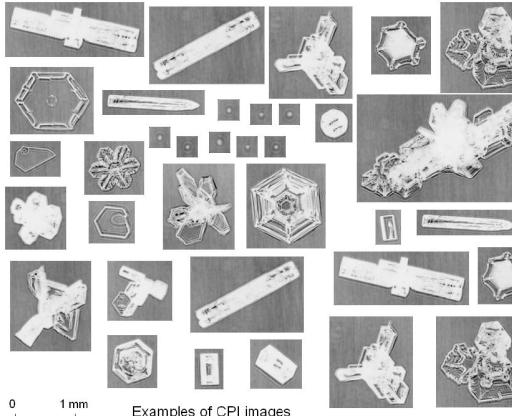
# Introduction: the complexity of clouds

Processes responsible for formation and evolution of clouds are complex !



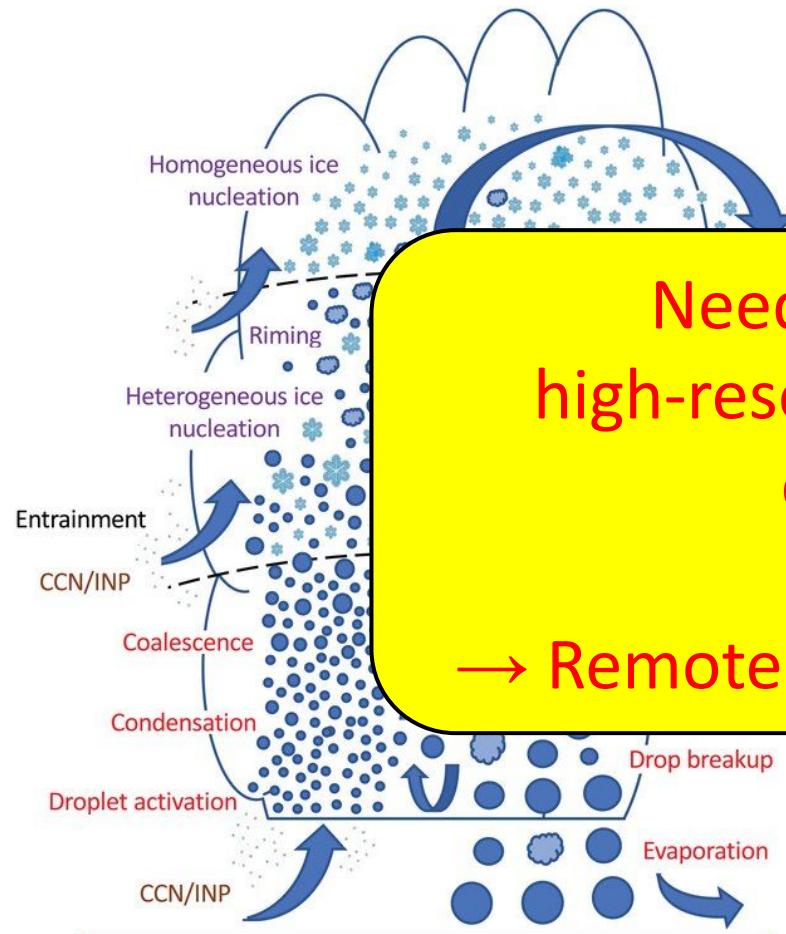
Morrison et al., 2020

<https://doi.org/10.1029/2019MS001689>



# Introduction: the complexity of clouds

Processes responsible for formation and evolution of clouds are complex !



Need for long-term &  
high-resolution vertical cloud  
observations

→ Remote sensing measurements

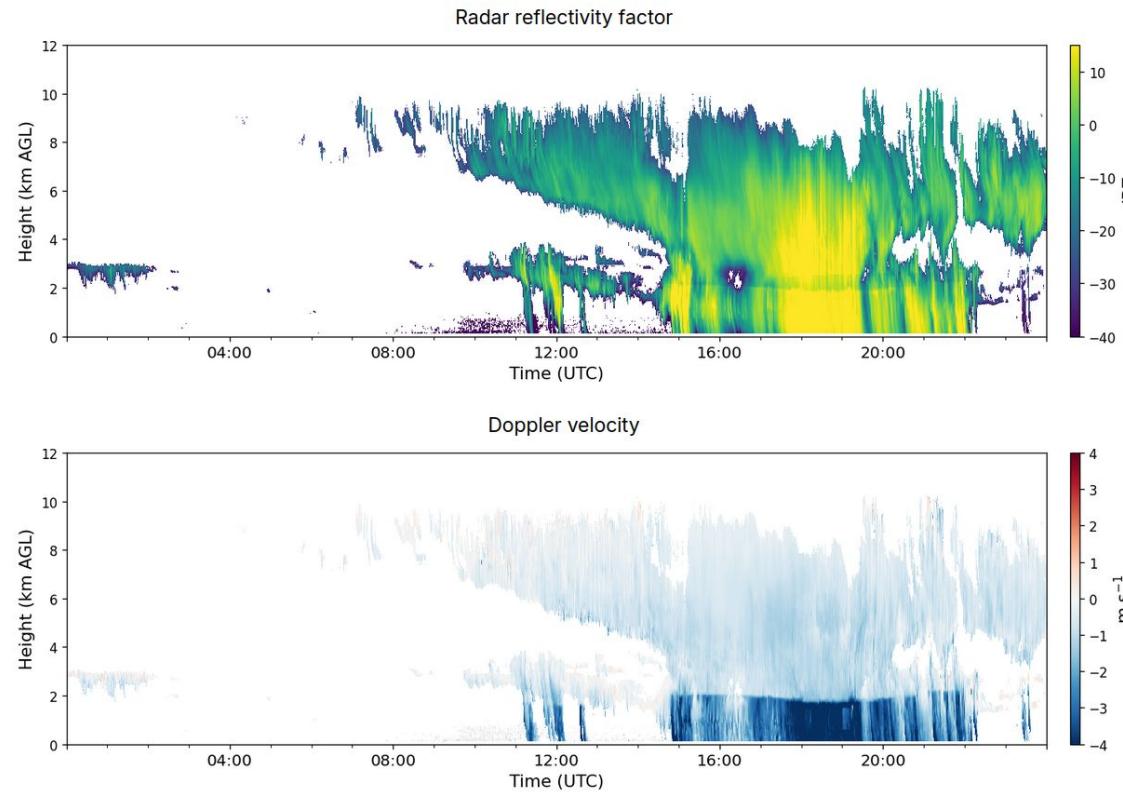
Morrison et al., 2020

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# Motivation

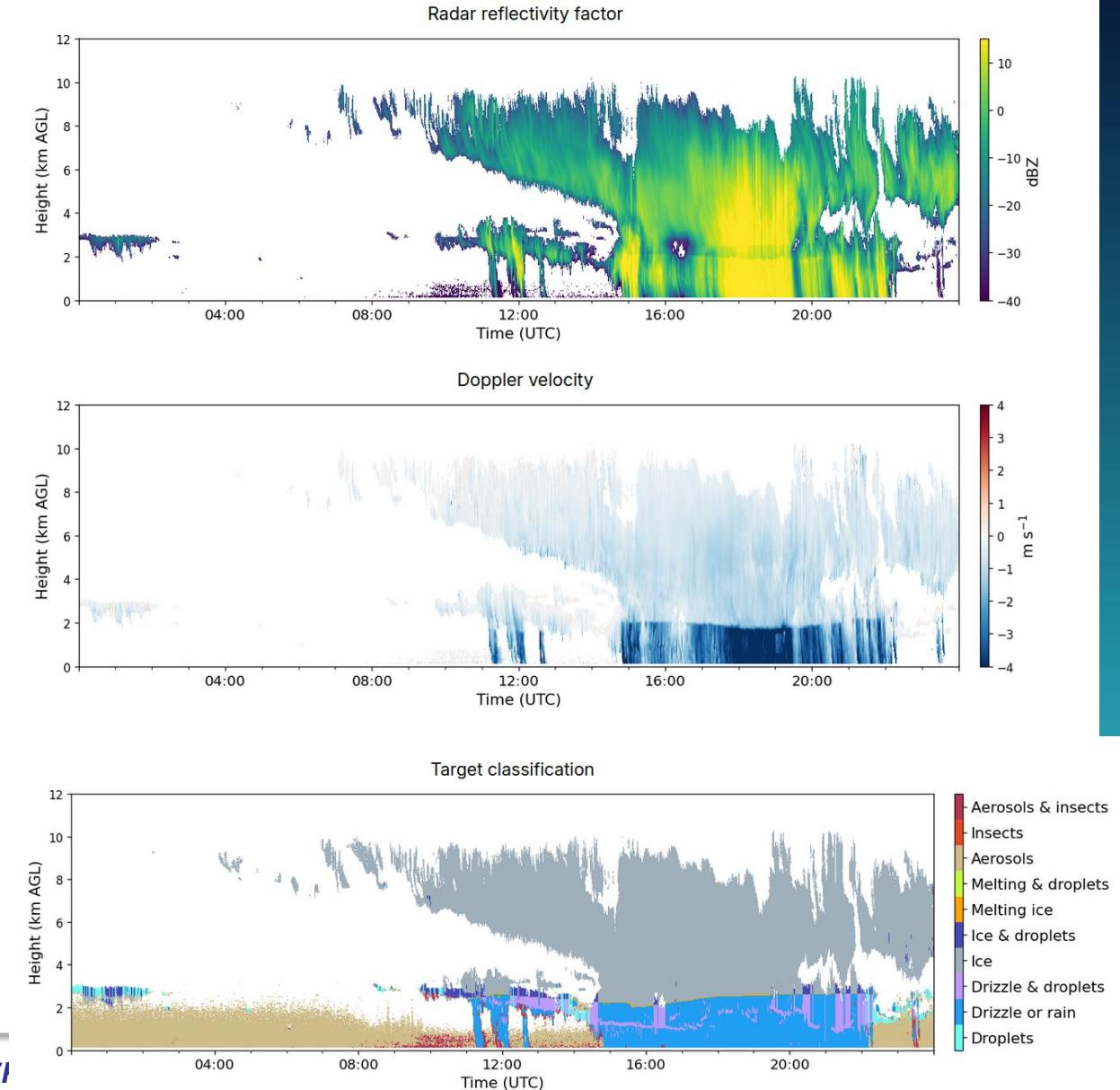
Granada, Spain  
20/01/2025  
<https://cloudbot.fmi.fi/>



# Motivation

Granada, Spain  
20/01/2025  
<https://cloudbot.fmi.fi/>

Remote sensing synergy →  
Level 2 product



# RADAR PRINCIPLES & CLOUD RADARS

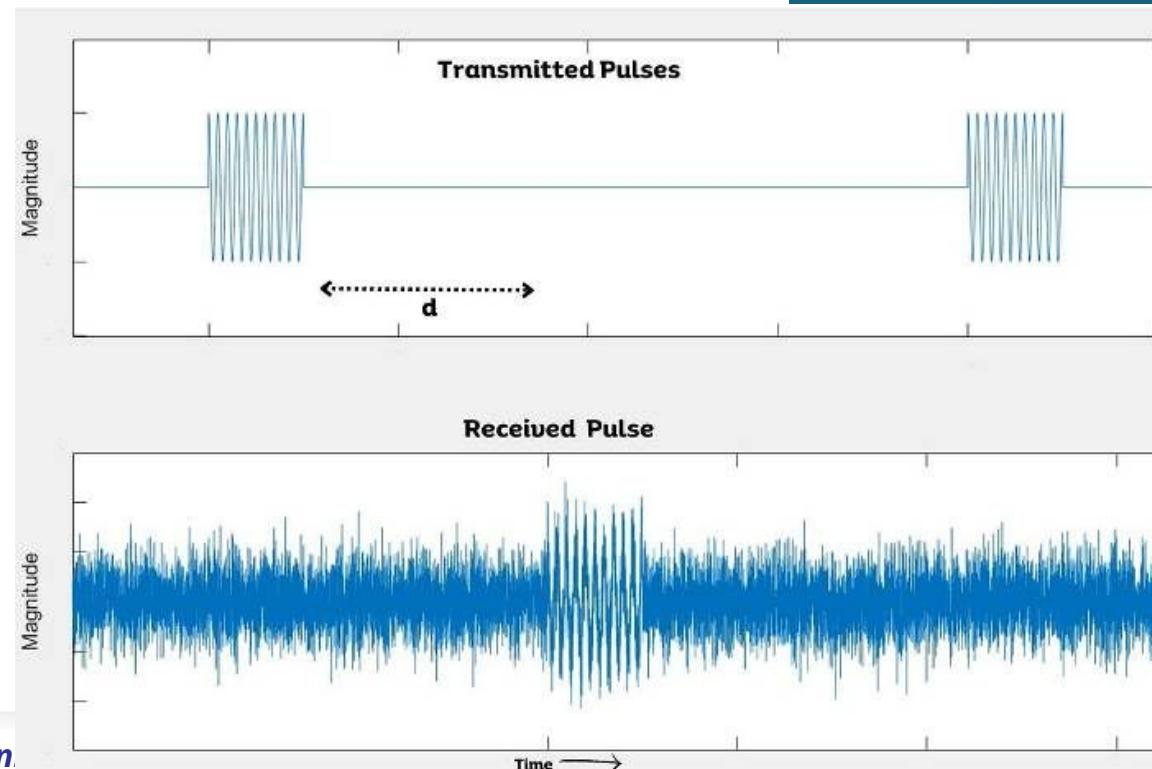
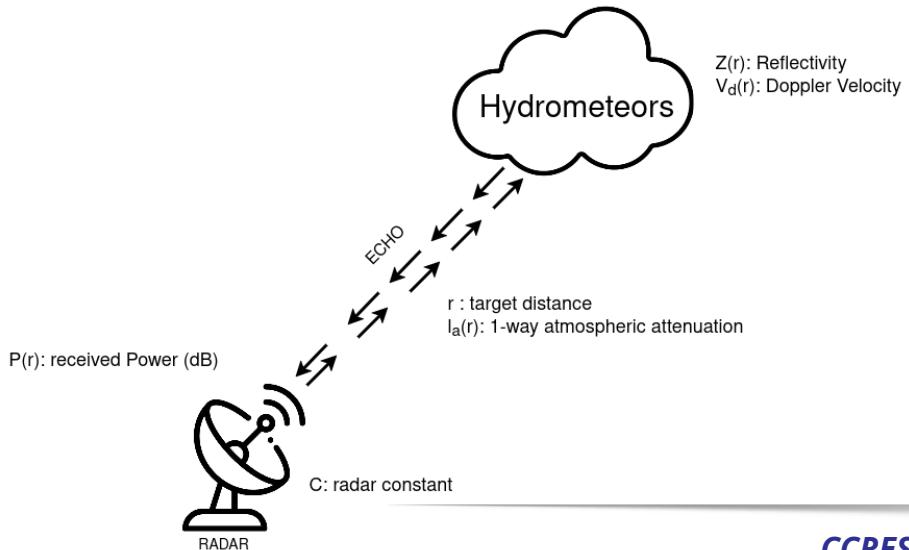
# I - Main principles of radar

**RADAR** = **R**adio **D**etection **A**nd **R**anging

## Active remote sensing

A radar system has 2 main functions:

1. **Transmission** of pulsed/continuous radiation in a specific direction
2. **Detection** of the radiation reflected by the target
  - a. Intensity and phase of the signal (detection)
  - b. Distance and location (ranging)



# I - Main principles of radar

What do we measure with a radar ?

How can we use EM waves ?

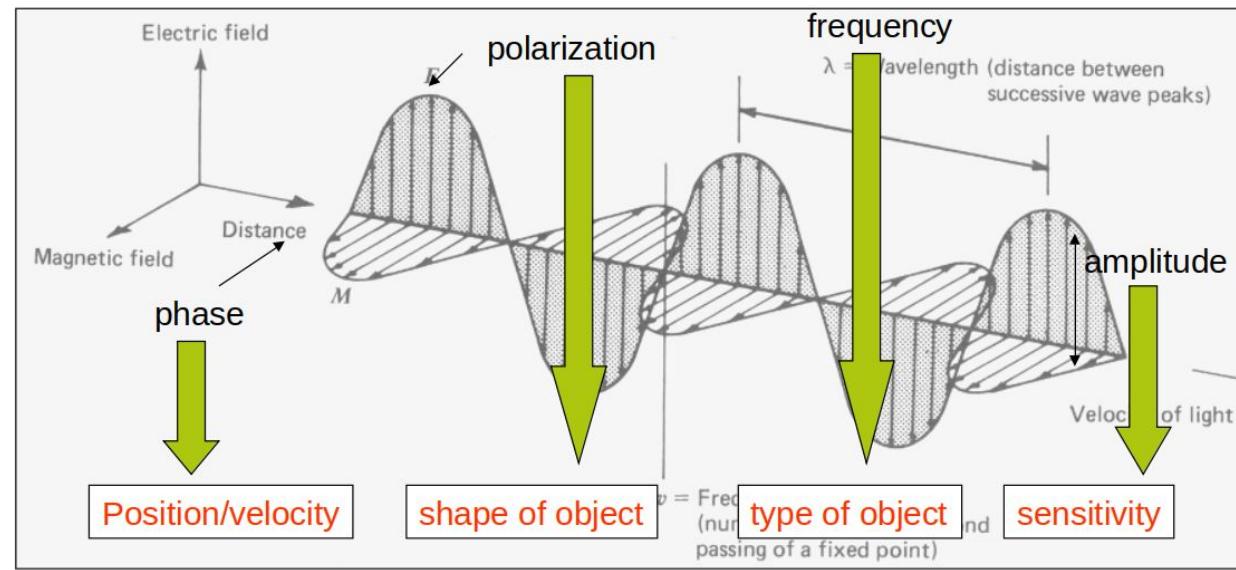
**Inverse problem:** measures signal reflected by hydrometeors, but we seek to retrieve cloud structure and content

An EM wave can be described mathematically as:

$$s(t) = A \cos(2\pi f \cdot t + \varphi)$$

- **Frequency (f)** → determines sensitivity to particle type/size
- **Amplitude (A(t))** → related to reflectivity, indicates concentration of hydrometeors ( $\text{Power} \propto A^2$ )
- **Phase ( $\varphi$ )** → gives position and velocity (via time delay and Doppler shift)
- **Polarization** → reveals shape of particles (e.g. raindrops vs ice crystals)

→ Radar measures how the wave is modified by the cloud, and infers its structure, content, and motion

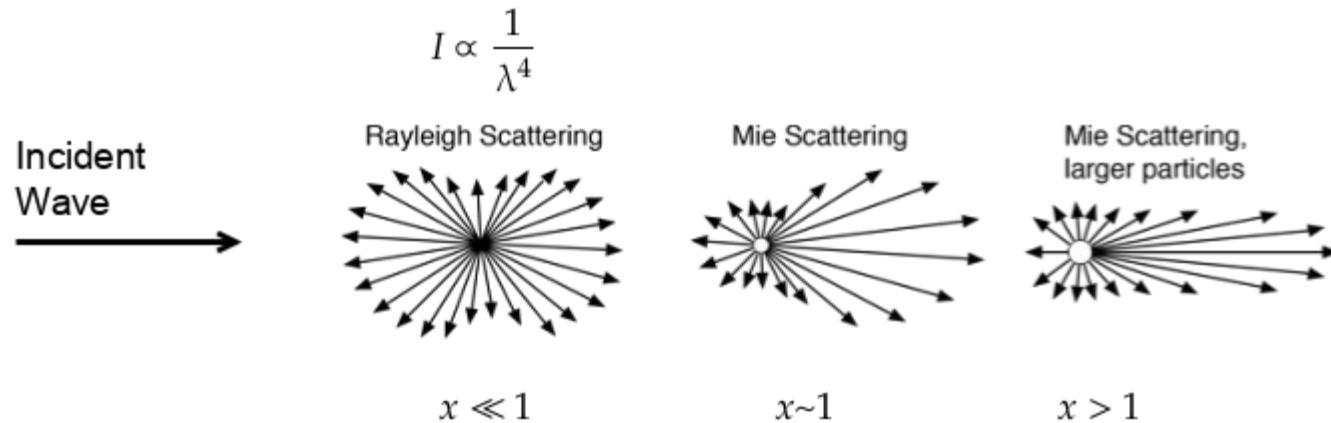


From H. Russchenberg  
TU Delft Master lesson on cloud radar 2015

# I - Wave Scattering

- Size parameter :

$$x = \frac{\pi D}{\lambda}$$



The standard radar equation assumes that the particle diameter/wavelength ratio is in the Rayleigh scattering range. In this case, the radar cross section for a single particle is:

$$\gamma_v(D) = \frac{\pi^5 K^2}{\lambda^4} D^6$$

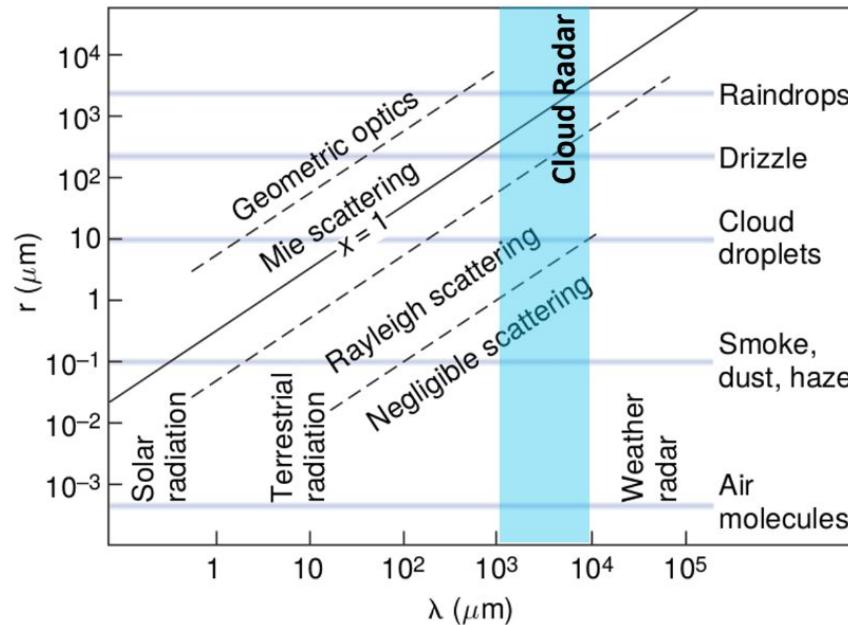
$K^2 = (\varepsilon_r - 1)^2 / (\varepsilon_r + 2)^2$  is the dielectric factor, depends on particles complex relative permittivity  $\varepsilon_r$

Typically  $K^2 = 0.86$  or  $= 0.75$

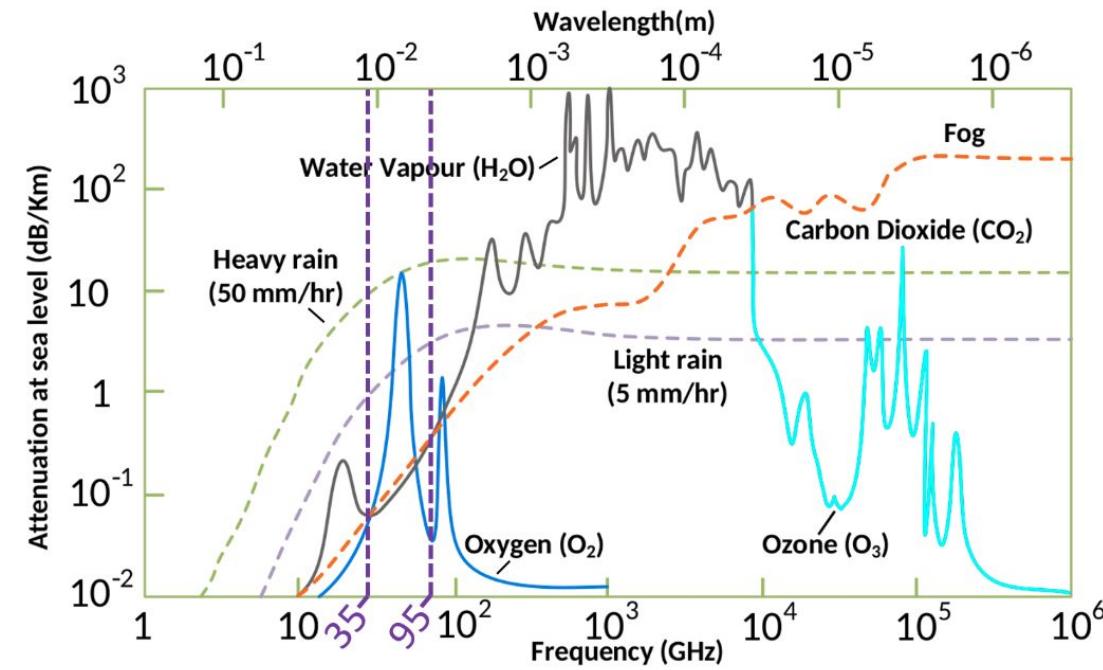
# I - Main principles of radar: Cloud radars frequency band

- They usually operate in the
  - Ka band (~35 GHz):** ~ 3mm
  - W band (~95 GHz):** ~ 9mm
- Rayleigh scattering** with **cloud particles (10-100μm)**
- Lower atmospheric attenuation, “atmospheric windows”

(a) Scattering regime versus wavelength and particle radius



(b) Electromagnetic absorption of different atmospheric components versus frequency



## II - Cloud Radar types

- Frequency-modulated continuous wave (**FMCW**) vs. **Pulsed**
- **Single / Double** polarization
- **Vertical pointing** vs **scanning**
- **Differ in terms of:** operation mode, capabilities, data quality, size/weight, advanced products

RPG	BOWEN	METEK
FMCW-94/35	BASTA	MIRA-35
35-94GHz / 94GHz	94 GHz	35 GHz
FMCW	FMCW	Pulsed

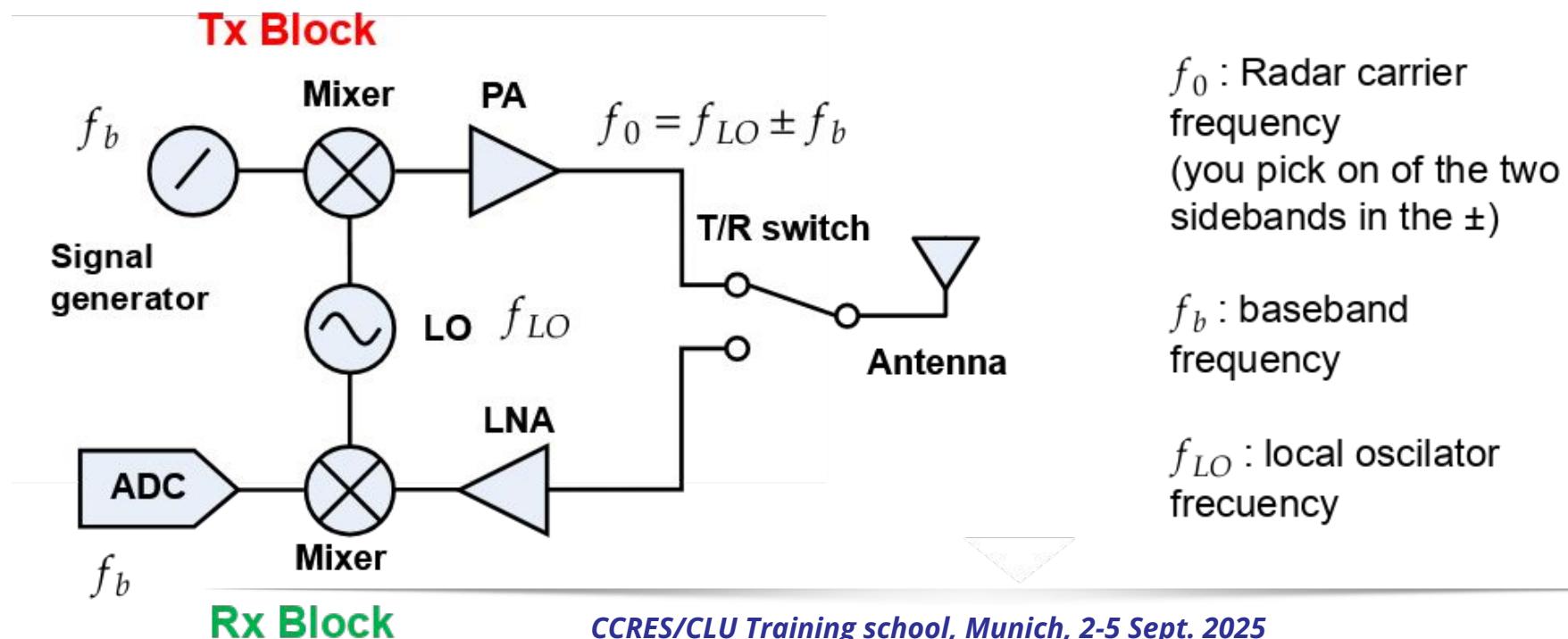


I, Munich, 1

# II - Radar Hardware

## Hardware overview

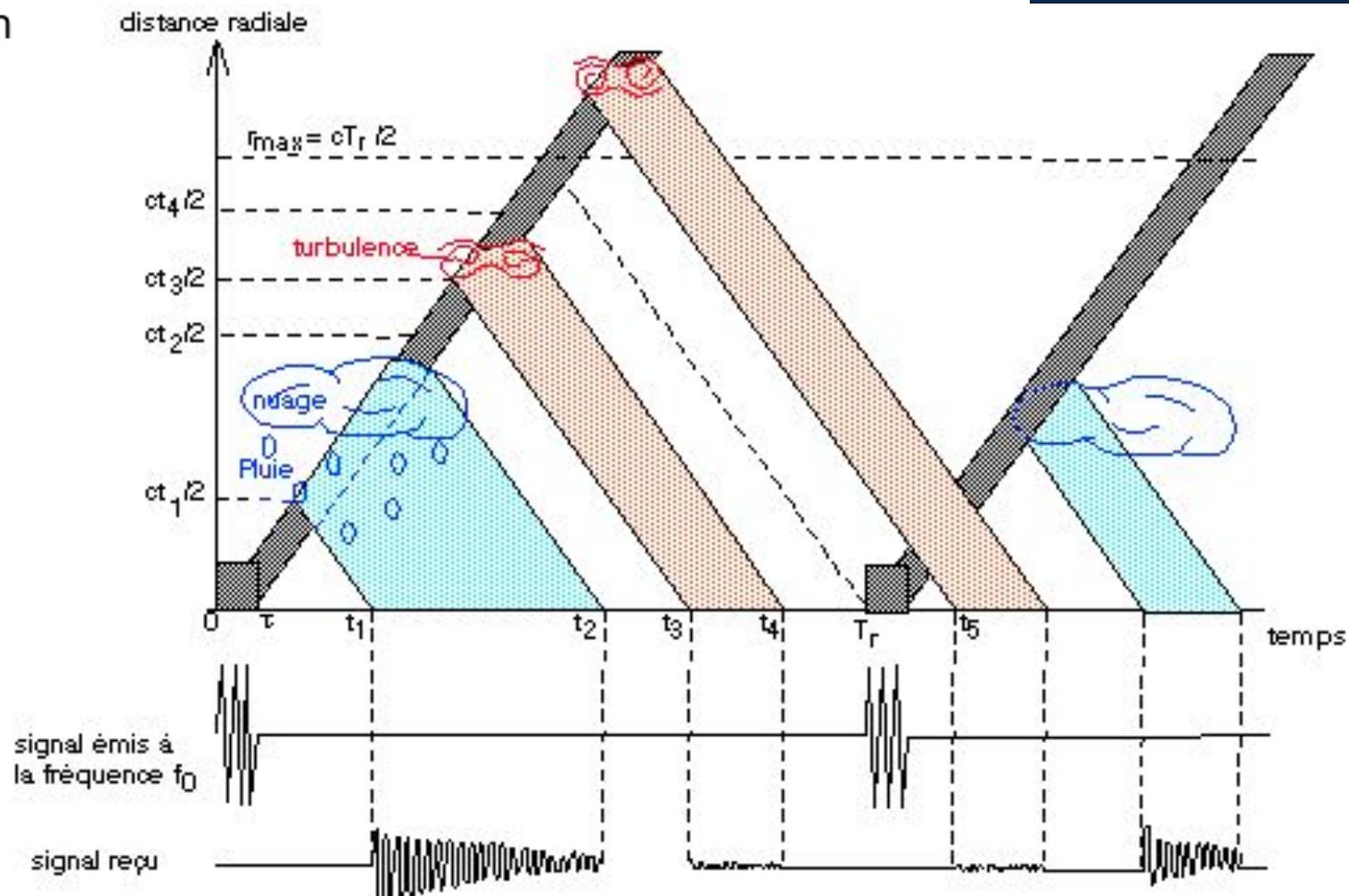
- Pulsed and FMCW radars have **transmitter** and **receiver** blocks
- There is a very large number of possible architectures and implementations that can work as a radar. However, many of them have some key components in common.
- Frequency generation and conversion stages are usually implemented with **mixers** and **local oscillators (LO)**, and RF chains include **power amplifiers (PA)** and **low noise amplifiers (LNA)** to increase the instrument sensitivity.



# Pulsed Radar Operation

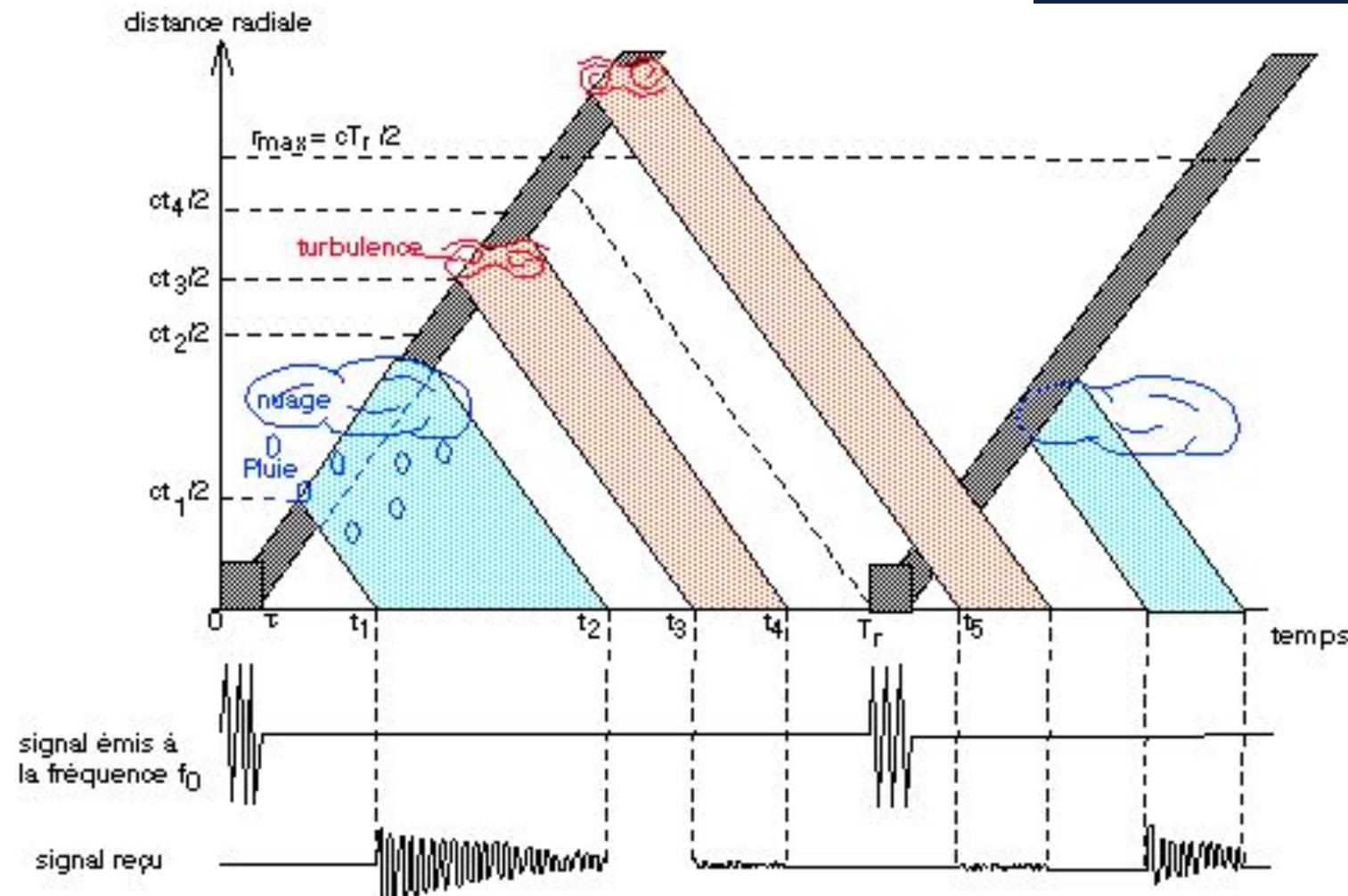
## Operation of a pulsed radar

- The pulsed radar emits pulses with a duration of  $\tau$ , a frequency  $f_0$  and mean power  $P_t$
- Suppose a signal that bounces back with a time delay  $t$  from the pulse generation
- Range to the object:
  - $r = ct/2$
- Range resolution:
  - $\delta r = c\tau/2$
- Blind range or zone, the pulse hides other signals:
  - $r_{min} = c\tau/2$
- Unambiguous range
  - $r_{max} = cT_r/2$
  - $T_r$  = Pulse repetition time (PRT)
  - $F_r = 1/T_r$  = Pulse repetition frequency (PRF)



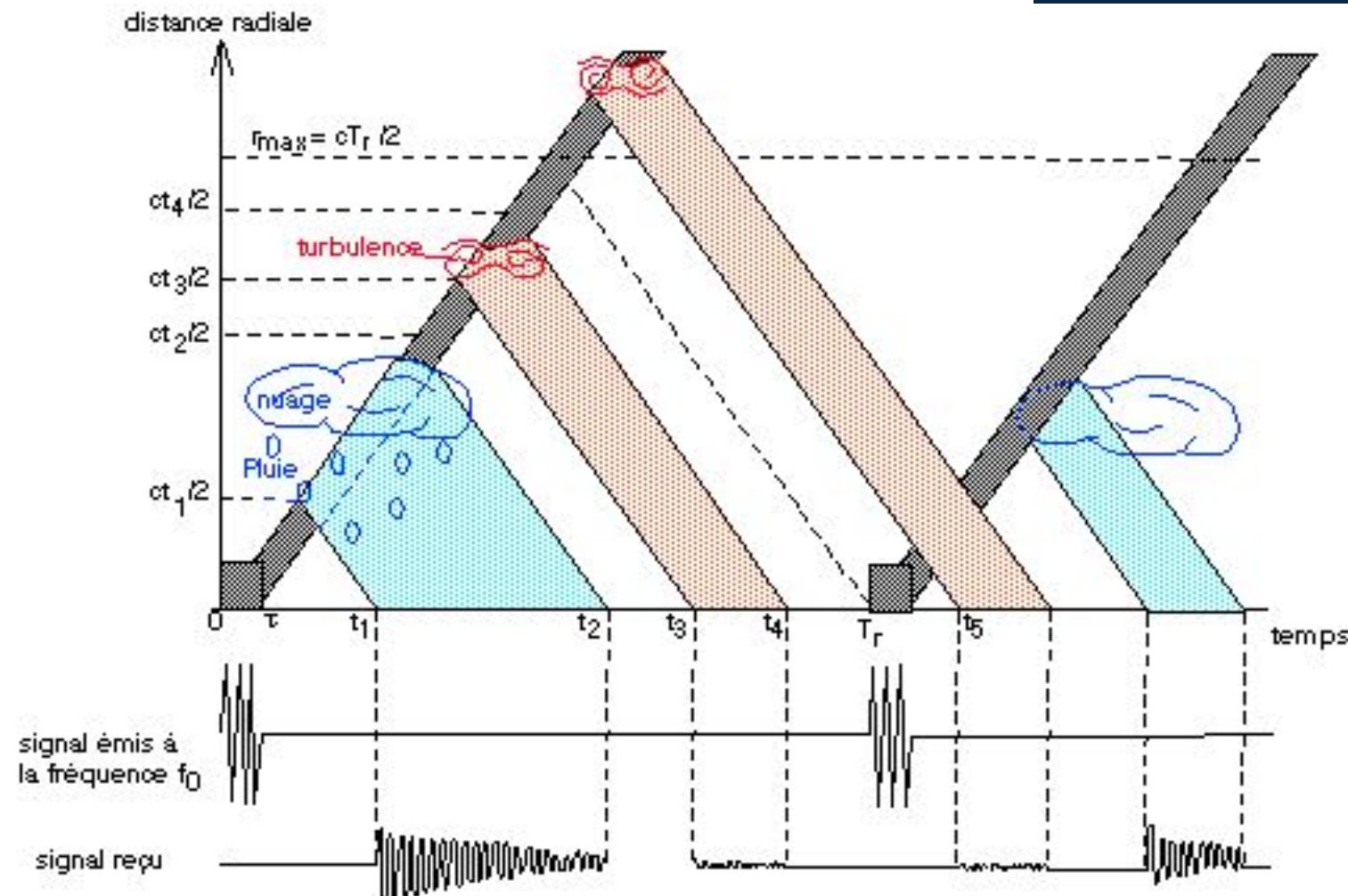
# Pulsed Radar Operation

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  - PRT =  $1 / \text{PRF}$
- Radars usually have high PRFs, to increase power output, enable coherent integration and improve doppler velocity estimates
  - For weather radars it can be of several hundred Hz to several kilohertz



# Pulsed Radar Operation

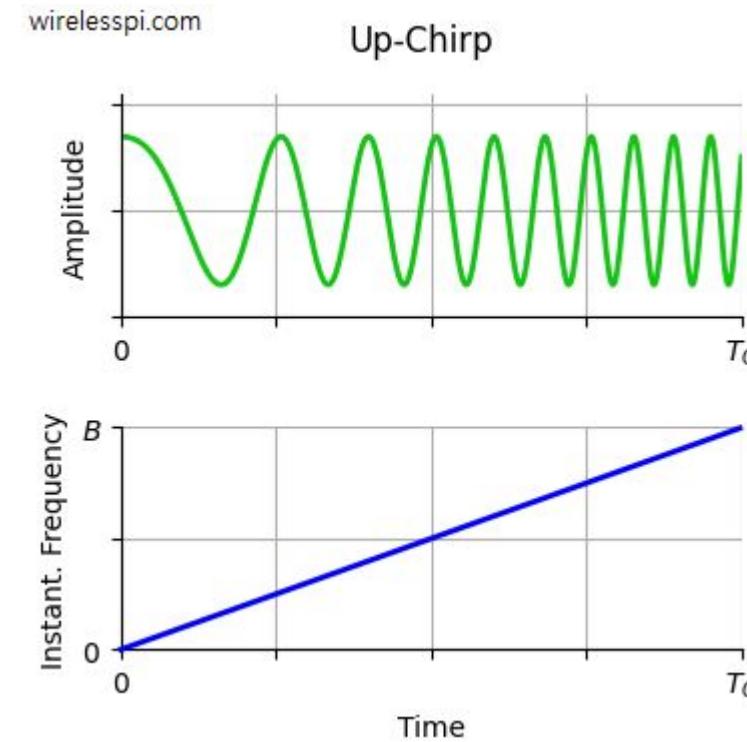
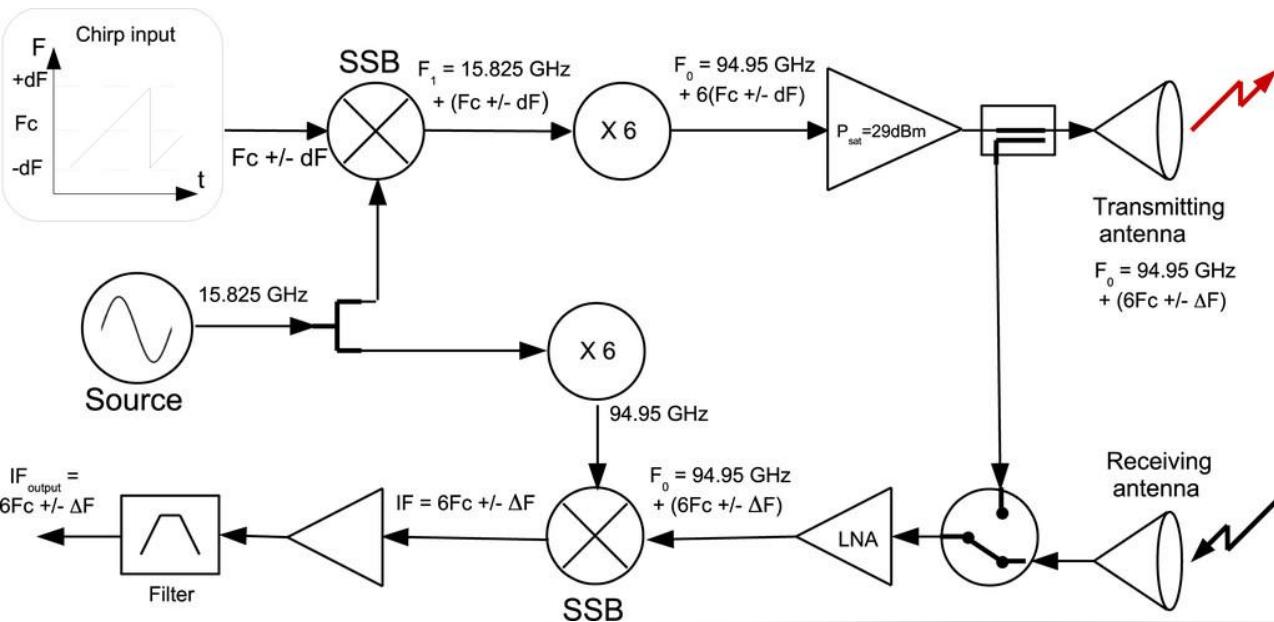
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# FMCW Radar Operation

- FMCW = Frequency Modulated Continuous Wave
- Instead of “pulses” it continuously transmits “chirps” of a signal modulated in frequency
- The **frequency** difference between the transmitted and received signal gives **range**
- The **phase** evolution from chirp gives **Doppler velocity**

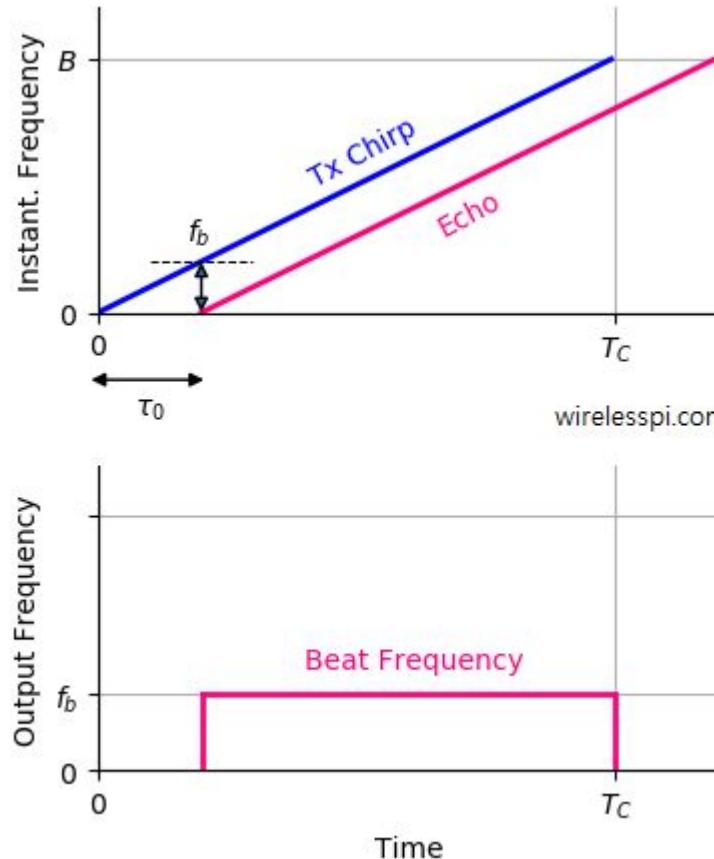
Example of a FMCW radar architecture, BASTA radar, Delanoë et al. 2016.



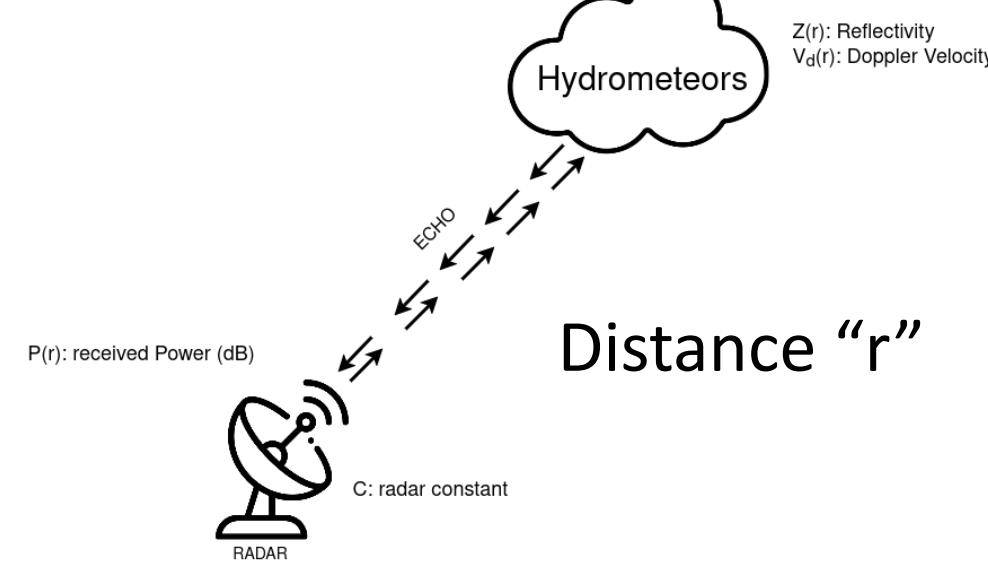
Single chirp:  
The emitted signal frequency increases

# FMCW Radar Operation

- Travel time  $\tau_0$  : time it takes for a round trip.
- The travel time produces a frequency difference between transmitted and received signals → This is the “beat frequency”  $f_b$
- By **mixing** the transmitted and received signals we get a “beat signal”. The frequency components will have information on range

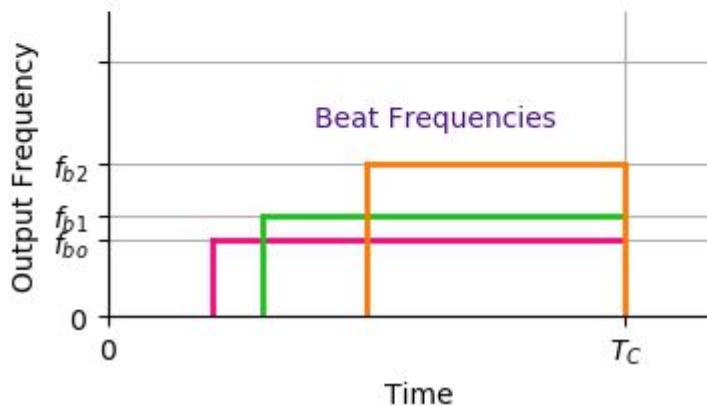
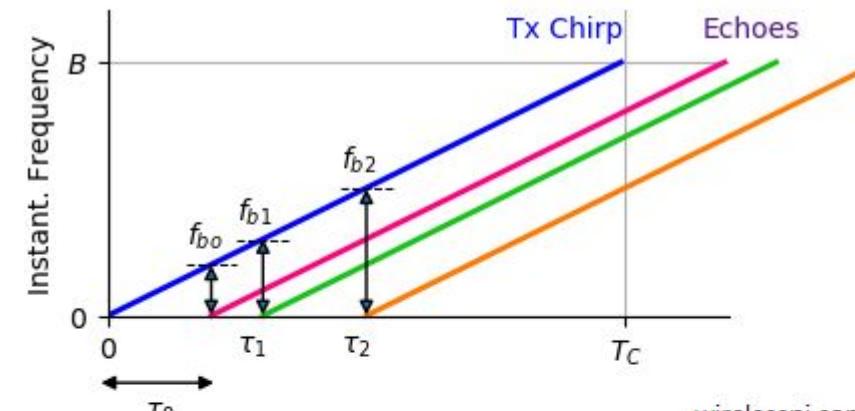
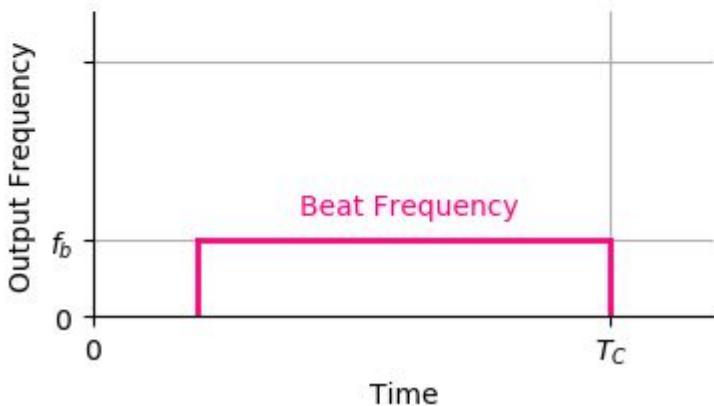
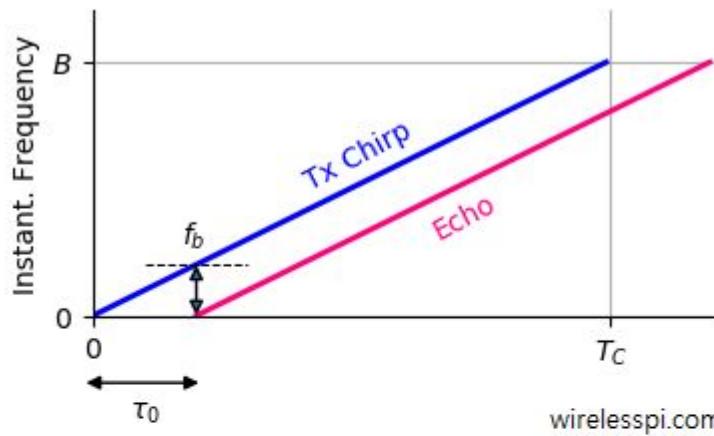


$$\tau_0 = \frac{2r}{c}$$



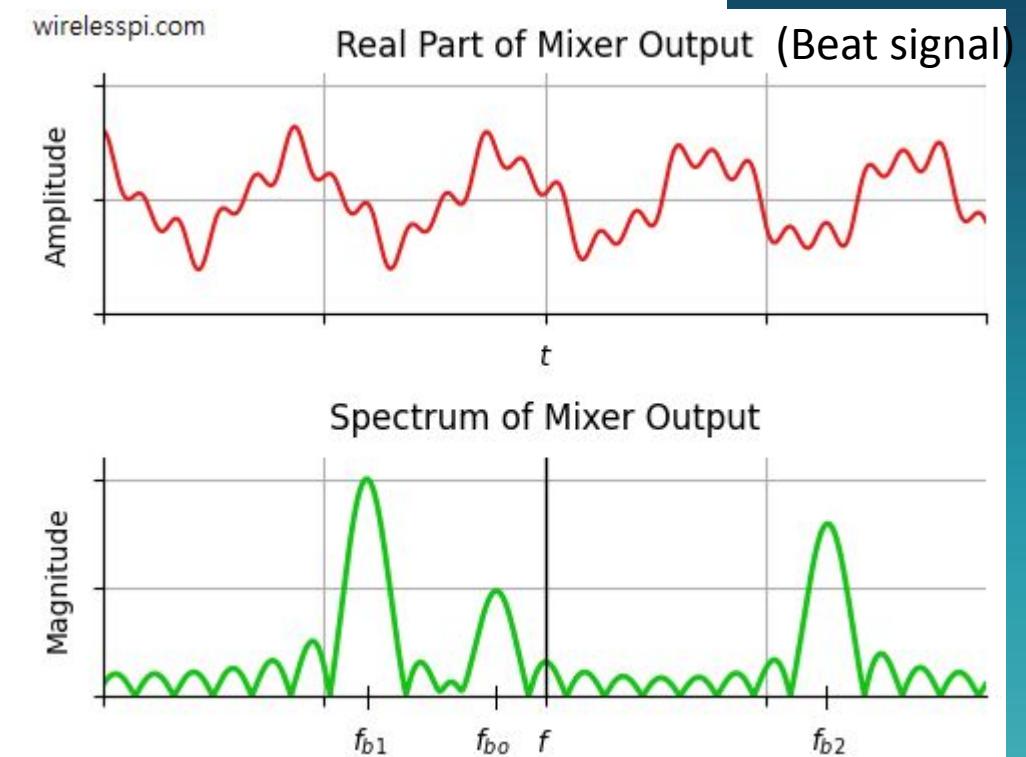
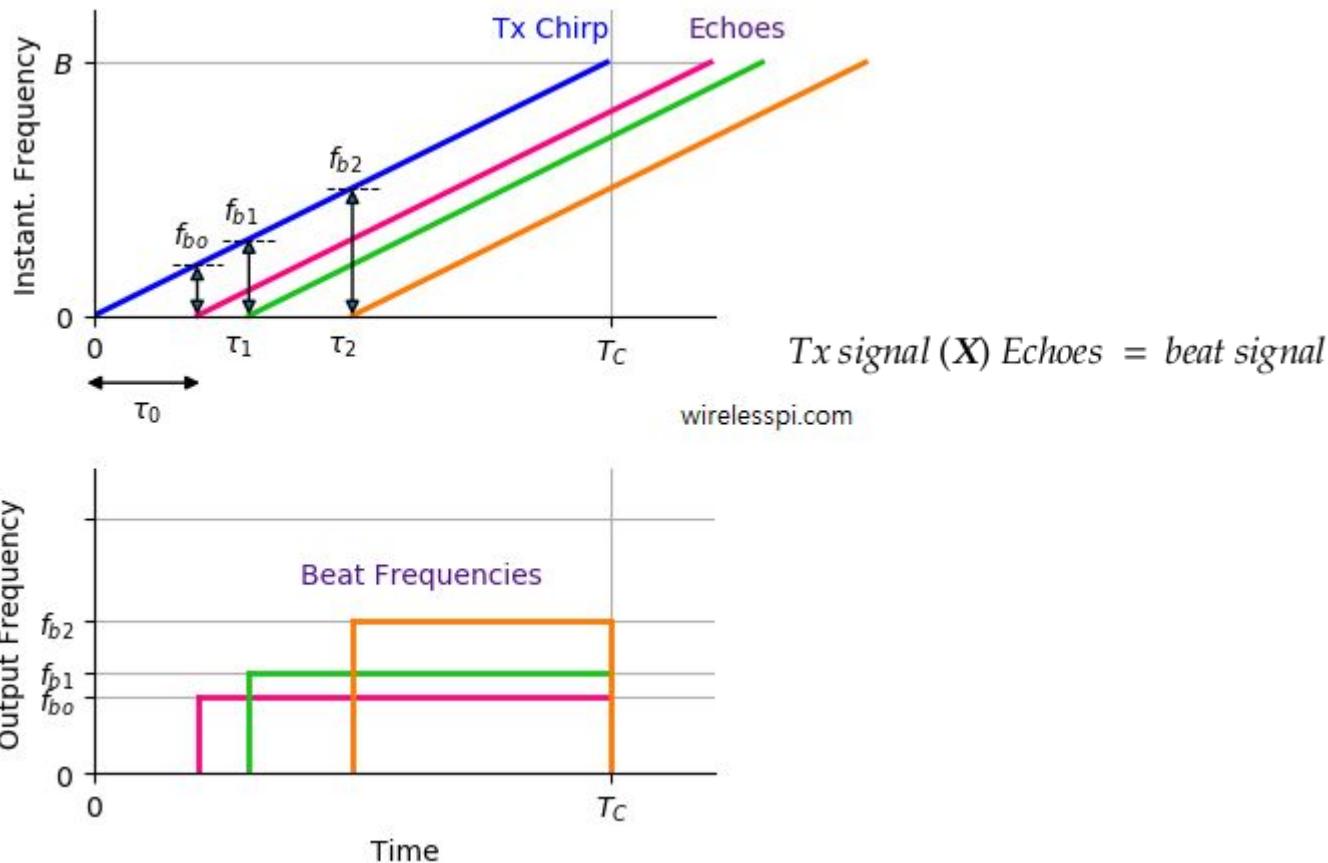
# FMCW Radar Operation

- The time  $\tau_0$  it takes for the round trip will produce a frequency difference between the transmitted and received signals. This is the “beat frequency”  $f_b$
- By mixing the transmitted and received signals we get a “beat signal”. The frequency components can be extracted from filtering + FFT treatment



# FMCW Radar Operation

- The time  $\tau_0$  it takes for the round trip will produce a frequency difference between the transmitted and received signals. This is the “beat frequency”  $f_b$
- By **mixing** the transmitted and received signals we get a “beat signal”. The frequency components can be extracted from filtering + FFT treatment



# FMCW Radar range equations

- As with pulsed radars, many chirps are sent in cadence during operation

Key equations:

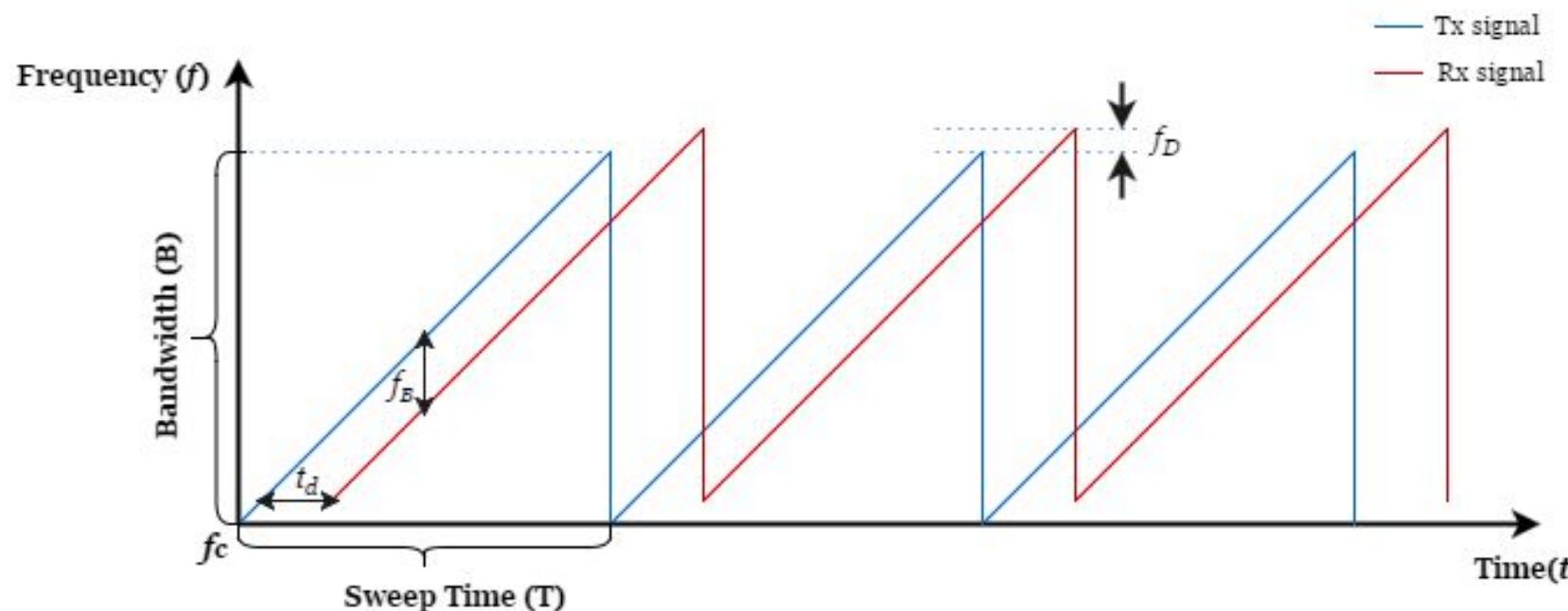
$$\text{Chirp frequency slope } \alpha = \frac{B}{T}$$

$$\text{Unambiguous range } r_{max} = \frac{cT}{2}$$

$$\text{Range } r = \frac{f_b c}{2\alpha}$$

$$\text{Range resolution } \Delta r = \frac{c}{2B}$$

Blindzone? Depends on the radar hardware, “crosstalk”

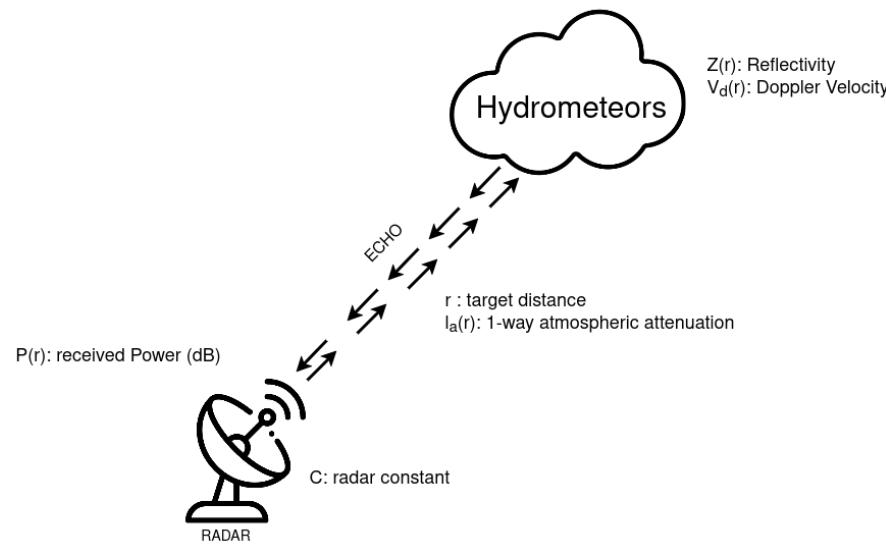


Suleymanov, S. (2016). *Design and Implement of an FMCW Radar Signal Processing Module for Automotive Applications* (Doctoral dissertation, Master Thesis, Aug. 31).

# RADAR EQUATION

# The Radar Equation

- The **radar equation** describes how **power scattered back** from atmospheric **hydrometeors** relates to their **physical properties** and **distance** from the radar
- In the case of **cloud radars**, we need it to calculate **key** radar **parameters** such as the **Radar Cross Section (RCS)** and the **Radar Equivalent Reflectivity (Z)**



ADD vertical  
reflectivity profile and  
a scan

# The Radar Equation

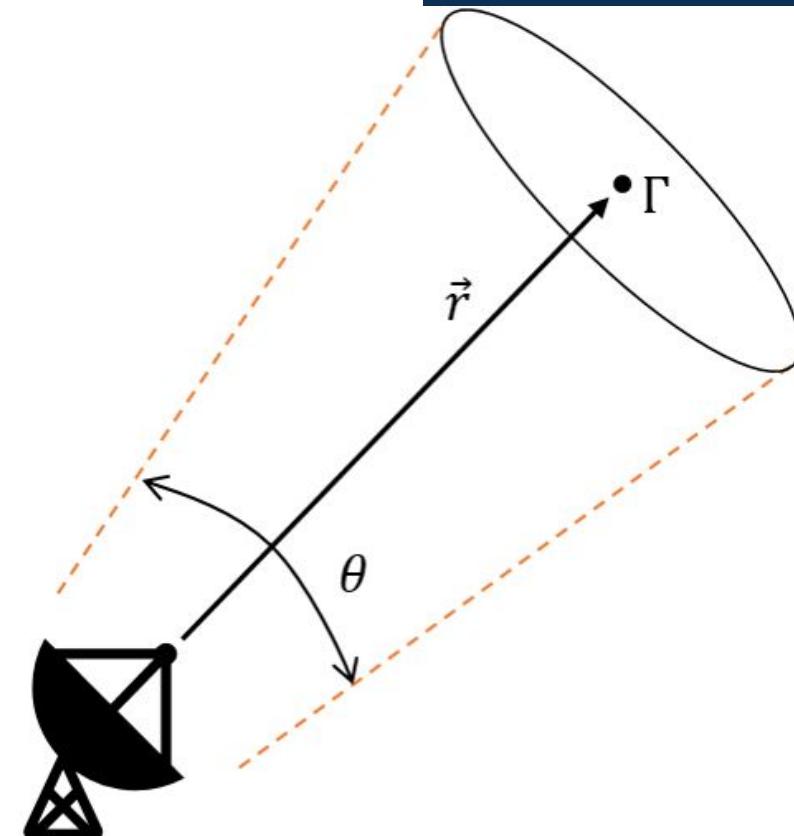
- Power received at the target position  $\vec{r}$  :

$$P_{\text{inci}}(\vec{r}) = \frac{P_t G_a}{4\pi r^2 l_a(r)}$$

- Incident power :  $P_{\text{inci}}(\vec{r})$  [mW] ; Transmitter power :  $P_t$  [mW]
- Max. antenna gain :  $G_a$
- Atmospheric attenuation from the radar to  $\vec{r}$  :  $l_a(r)$
- The target has a radar cross section  $\Gamma$  [ $\text{m}^2$ ]
- Power scattered back and received by the radar, from the target at  $\vec{r}$  :

$$P_r(\vec{r}) = P_{\text{inci}}(\vec{r}) \frac{A_p}{4\pi r^2 l_a(r)} \Gamma = \frac{P_t G_a}{4\pi r^2} \frac{A_p}{4\pi r^2} \frac{\Gamma(r)}{l_a^2(r)}$$

- $A_p$  is the effective antenna aperture for the receiver.



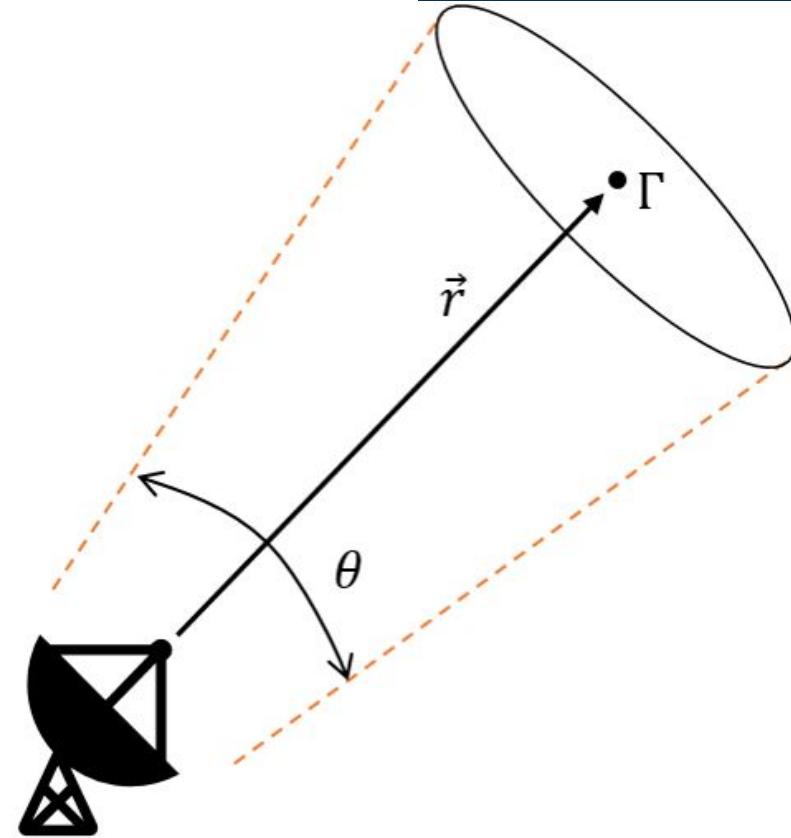
# The Radar Equation

$$A_p = \frac{G_a \lambda^2}{4\pi}$$

- $\lambda$  [m] : Radar wavelength
- With this information we get the radar equation for point targets\* :

$$P_r(\vec{r}) = \frac{G_a^2 \lambda^2 P_t}{(4\pi)^3 r^4 l_a^2(r)} \Gamma(r)$$

- By knowing the radar properties, we can measure the point target cross section from received power
- And what happens for distributed targets ?



\* The emitting and receiving antennas are assumed to have the same gain and axially symmetric beam lobes

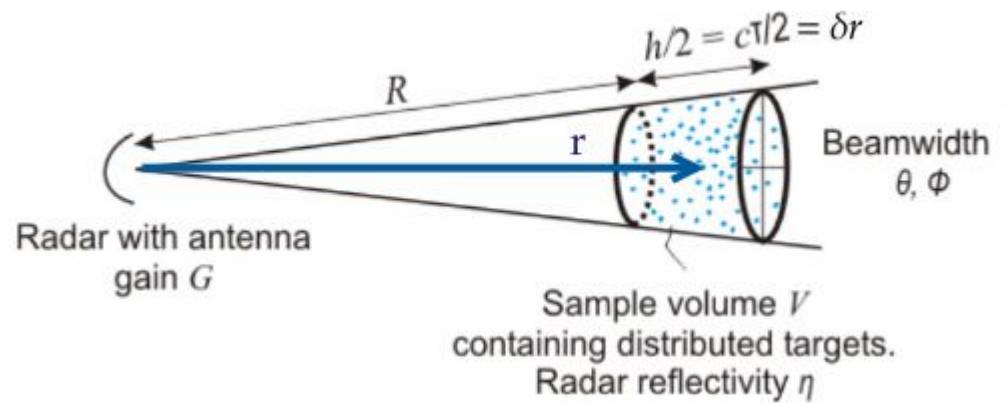
# Sampling volume

- If we assume that for each sampling volume we have a uniform droplet distribution  $N(D)$  [number/m<sup>3</sup>], then the total cross section would be :

$$\Gamma_v = V(r) \int_0^{\infty} N(D) \gamma_v(D) dD = V(r) \int_0^{\infty} \frac{\pi^5 K^2}{\lambda^4} N(D) D^6 dD$$

- The effective sampling volume is calculated as:

$$V(r) = \int_{r-\delta r/2}^{r+\delta r/2} \int_0^{\pi} \int_0^{2\pi} f_a^2(\theta, \phi) r^2 dr d\Omega \approx r^2 \delta r \int_0^{\pi} \int_0^{2\pi} f_a^2(\theta, \phi) d\Omega$$



Where  $f_a(\theta, \phi)$  is the normalized antenna pattern (antenna pattern divided by the maximum gain value). For symmetric antennas ( $\theta = \phi$ ) with Gaussian lobes :

$$V(r) = \frac{\pi r^2 \delta r}{2 \ln 2} \left(\frac{\theta}{2}\right)^2$$

# The radar Equation

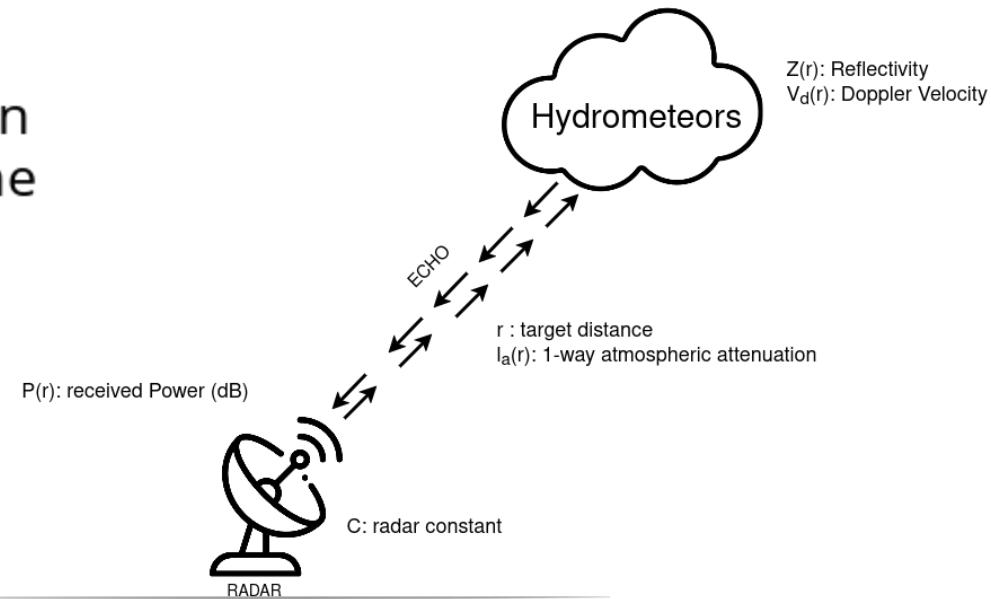
- Definition of radar equivalent reflectivity from the Droplet Size Distribution (DSD):

$$Z = \int_0^{\infty} N(D) D^6 dD \text{ [m}^6\text{m}^{-3}\text{]} = 10^{18} \int_0^{\infty} N(D) D^6 dD \text{ [mm}^6\text{m}^{-3}\text{]}$$

- The change to mm units is because these values are more commonly found in DSD measurements for precipitation
- Using the definition of  $Z$  and  $\Gamma_v$ , we can replace the RCS in the point target equation to get the radar equation for the **reflectivity** of distributed targets :

$$P_r(\vec{r}) = \frac{G_a^2 \lambda^2 P_t}{(4\pi)^3 r^4 l_a^2(r)} \Gamma_v = \frac{10^{18} \pi^3 \theta^2 G_a^2 P_t \delta r}{512 \lambda^2 \ln 2} \frac{K^2}{l_a^2(r) r^2} Z(\vec{r})$$

$Z$  in  $\text{mm}^6/\text{m}^3$



# The Radar Equation : Real Situation

- For real radars, the emitter and receiver can have different gains and losses that must be accounted for.

In reality  $P_t = P_t^{nom} / L_t$  ;  $P_t^{nom}$  : nominal transmitted power ;  $L_t$  : Transmitter losses

Example from the  
BASTA radar  
system  
Delanoë et al.  
2016

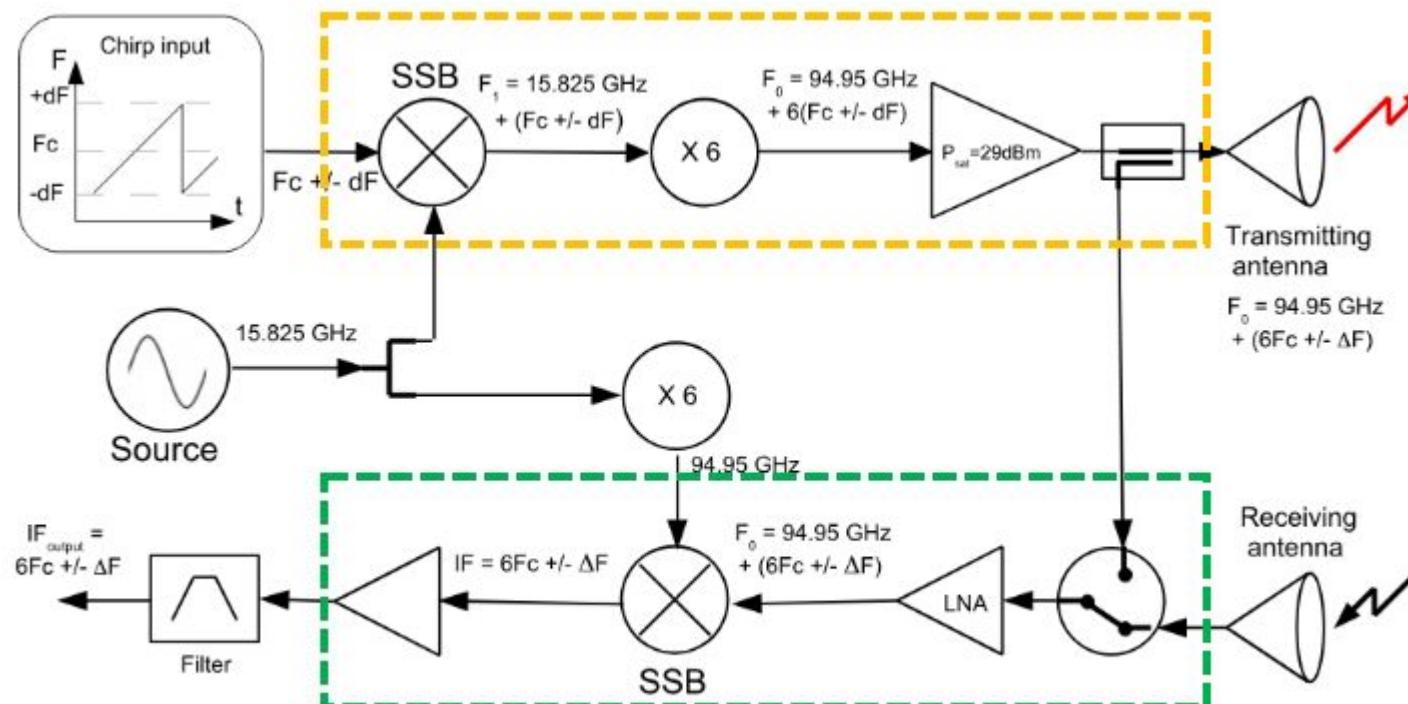


FIG. 8. Radar block diagram.

And similarly  $P_r^{meas}(r) = G_r P_r(r)$  ;  $P_r^{meas}(r)$  : measured received power ;  $G_r$  : Receiver gain

# The Radar Equation : Real Situation

- Considering radar gain and losses, the radar equation for point target becomes :

$$P_r^{meas}(\vec{r}) = \frac{G_a^2 \lambda^2 \mathbf{G}_r P_t}{(4\pi)^3 \mathbf{L}_t l_a^2(r) r^4} \Gamma = \frac{1}{c_\Gamma} \frac{\Gamma(r)}{l_a^2(r) r^4} \Rightarrow \Gamma(r) = c_\Gamma l_a^2(r) r^4 P_r^{meas}(\vec{r})$$

- And for reflectivities :

$$P_r^{meas}(\vec{r}) = \frac{10^{18} \pi^3 \theta^2 G_a^2 P_t^{nom} \delta r \mathbf{G}_r}{512 \lambda^2 \ln 2 \mathbf{L}_t} \frac{K^2}{l_a^2(r) r^2} Z_e(\vec{r}) = \frac{1}{c_z} \frac{Z_e(\vec{r})}{l_a^2(r) r^2} \Rightarrow Z_e(\vec{r}) = c_z l_a^2(r) r^2 P_r^{meas}(\vec{r})$$

- By knowing  $c_\Gamma$  and  $c_z$  we can calculate  $\Gamma$  and  $Z_e$  from radar measurements!  
→ Radar calibration

# The Radar Equation : Real Situation

- Considering radar gain and losses, the radar equation for point target becomes :

$$P_r^{meas}(\vec{r}) = \frac{G_a^2 \lambda^2 \mathbf{G}_r P_t}{(4\pi)^3 L_a l^2(r) r^4} \Gamma = \frac{1}{c_\Gamma} \frac{\Gamma(r)}{l^2(r) r^4} \Rightarrow \Gamma(r) = c_\Gamma l_a^2(r) r^4 P_r^{meas}(\vec{r})$$

- And for reflection

$$P_r^{meas}(\vec{r}) = \frac{10^{18} \pi^3 \theta^2}{512 \lambda^4} \Gamma(r) r^2 P_r^{meas}(\vec{r})$$

Hands on Training on Radar  
Calibration this afternoon

- By knowing  $c_\Gamma$  and  $c_z$  we can calculate  $\Gamma$  and  $Z_e$  from radar measurements!  
→ Radar calibration

# The Radar Equation : dB form

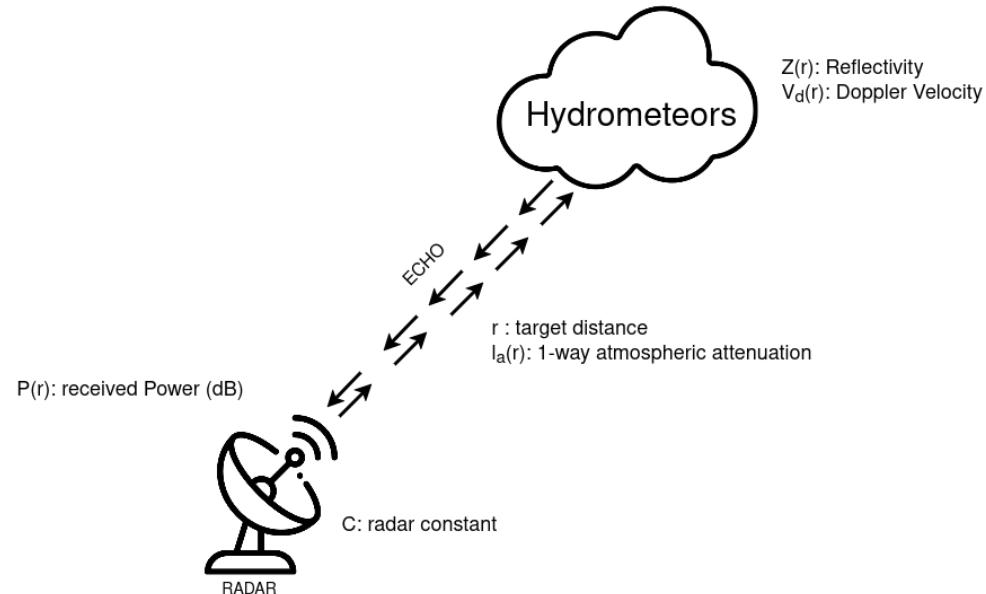
- To finalize, usually the radar equations are presented in dB form. Applying  $10 \log_{10}(\cdot)$  at both sides of the equation we get:

$$\Gamma(\mathbf{r})[\text{dBm}^2] = C_\Gamma + 2L_a(\mathbf{r}) + 40 \log_{10}(r[m]) + P_r^{\text{meas}}(\mathbf{r}) [\text{dBm}]$$

$$Z(\mathbf{r})[\text{dBZ}] = C_z + 2L_a(\mathbf{r}) + 20 \log_{10}(r[m]) + P_r^{\text{meas}}(\mathbf{r}) [\text{dBm}]$$

- With :

- $L_a(\mathbf{r}) = 10 \log_{10}(l_a(\mathbf{r}))$
- $P_r^{\text{meas}}(\mathbf{r}) = 10 \log_{10}(P_r^{\text{meas}}(\mathbf{r}))$
- $\Gamma(\mathbf{r}) = 10 \log_{10}(\Gamma(\mathbf{r}))$
- $Z(\mathbf{r}) = 10 \log_{10}(Z(\mathbf{r}))$



# Doppler velocity

# Doppler velocity

- Goal: measure the radial velocity of hydrometeors
- Based on the Doppler effect: a shift in frequency due to motion of target relative to the radar
- In meteorological radars, the motion is relatively slow (~0-10m/s for cloud droplets, up to 30-40m/s for graupel/hail in convective clouds)
- The frequency shift is very small (few Hz/kHz), due to high transmitted frequency and low target speeds
- The classical Doppler frequency is hard to detect directly
- Radars detect phase changes between successive pulses backscattered from the same volume (pulse-pair method)
- Same approach on pulsed and FMCW radars. Phase shifts are used on the raw signal for pulsed, and on the beat signal for FMCW

# Doppler velocity estimation

- Only works if the radar is coherent, i.e. if it keeps track of the phase of emitted pulses
- The pulse has a wavelength  $\lambda_0$ , frequency  $f_0$ , starting phase of  $\varphi_0$
- The target has a radial velocity  $V_r$
- Pulse repetition period of  $T_r$

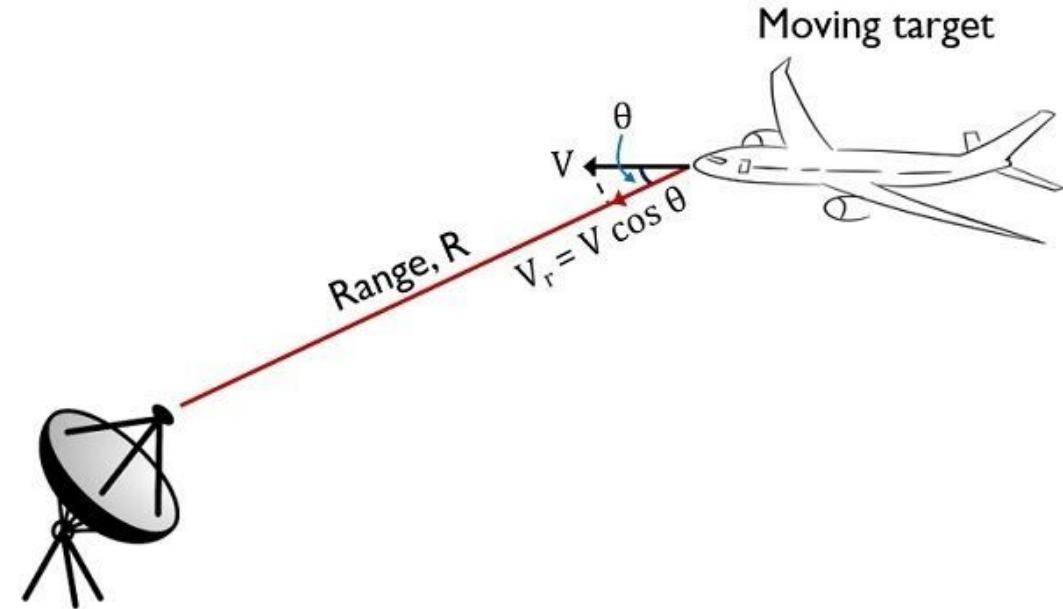
The angular excursion of a wave traveling between the radar and the target is of:

$$\Theta = 2\pi \cdot \frac{2R}{\lambda_0} = \frac{4\pi R}{\lambda_0}$$

The received signal would have the form:

$$s(t) = A(t) \cos(2\pi f_0 t + \varphi)$$

With  $\varphi = \Theta + \varphi_0$



Geometry of radar and target in deriving doppler frequency shift

Electronics Desk

Roshni Y., Doppler Effect in Radar, Electronics Desk

# Doppler velocity estimation

If the target moves, the phase at the receiver changes with time:

$$\varphi(t) = \frac{4\pi R(t)}{\lambda_0} + \varphi_0$$

Assuming that acceleration of the target is negligible at the radar time scale:

$$\frac{d\varphi(t)}{dt} = \frac{4\pi}{\lambda_0} \frac{dR(t)}{dt} \approx \frac{4\pi V_r}{\lambda_0}$$

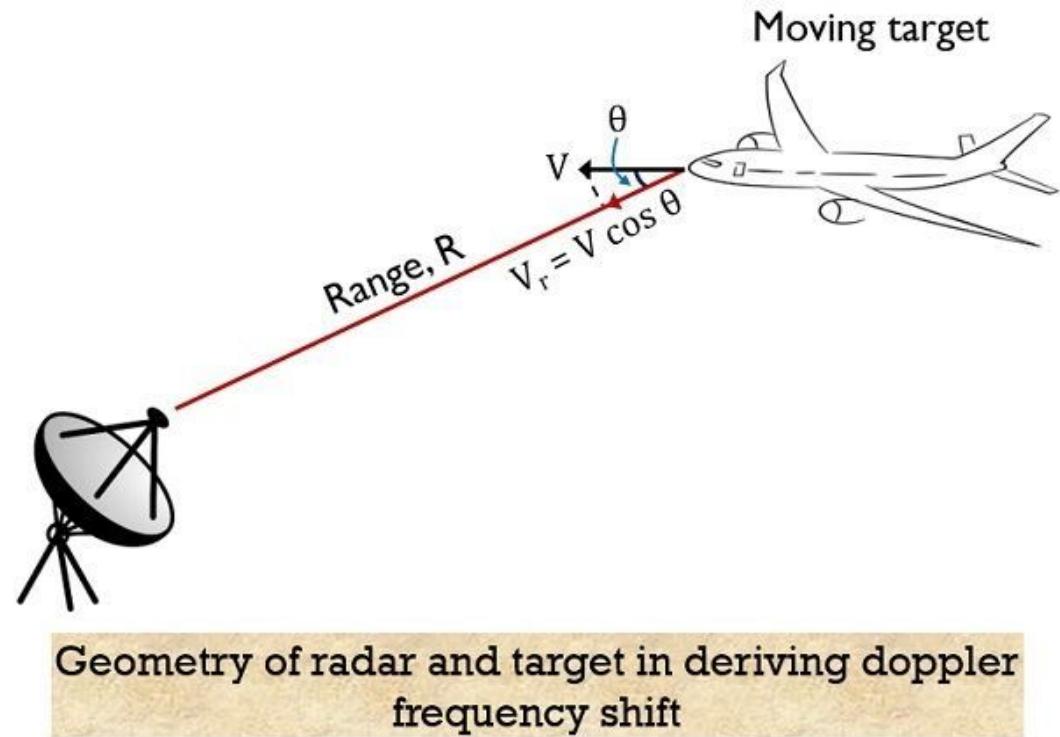
Hence, by sampling successive phase shifts we can estimate  $V_r$ :

$$V_r = \frac{\lambda_0}{4\pi} \frac{\Delta\varphi}{\Delta t} = \frac{\lambda_0}{4\pi T_r} \Delta\varphi$$

It can also be shown that, under these assumptions:

$$s(t) = A(t) \cos \left( 2\pi \left( 1 + \frac{2V_r}{c} \right) f_0 t + \varphi'_0 \right)$$

Doppler freq. shift



Electronics Desk

Roshni Y., Doppler Effect in Radar, Electronics Desk

# Doppler velocity estimation

If the target moves, the phase at the receiver changes with time:

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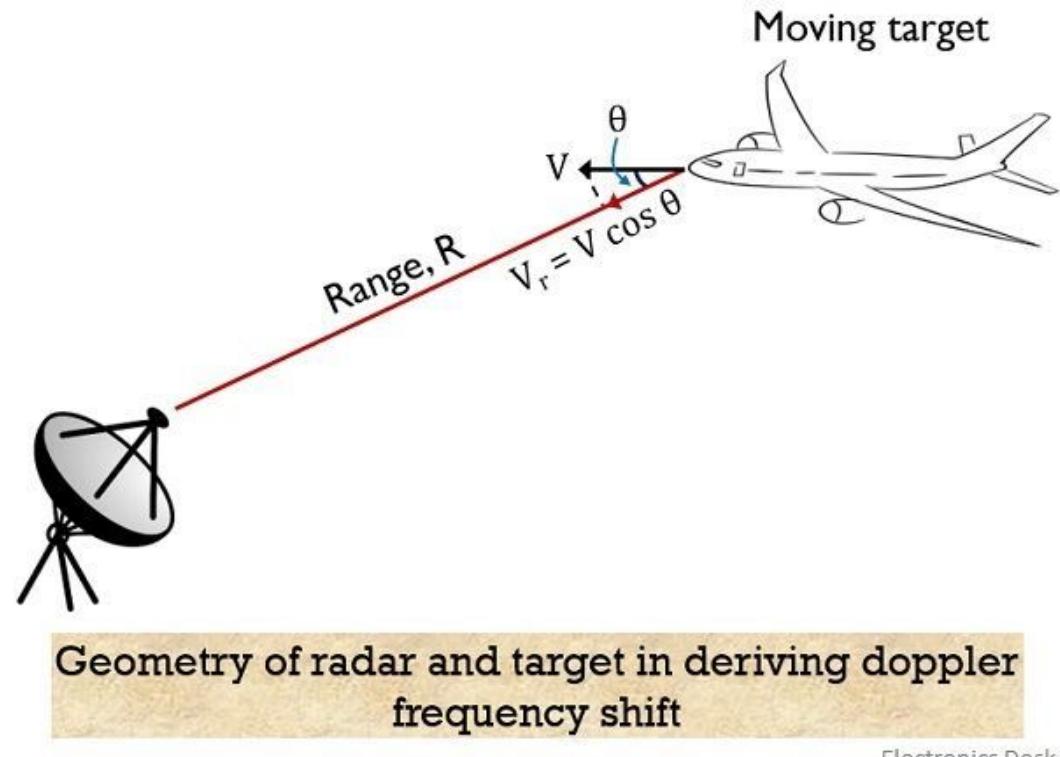
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Doppler freq. shift



Note: Notice the sign convention in the radial velocity! Weather radar conventions usually have this sign flipped, positive velocity means moving away from the radar.

# Doppler velocity estimation

## Unambiguous velocity

Sine waves are periodic, phase shift can be positive or negative  $\Rightarrow \Delta\varphi \equiv \Delta\varphi \pm \pi$

Thus, only phase shifts smaller than  $\pm \pi$  give **unambiguous** results

If  $|\Delta\varphi| < \pi$

$$\Rightarrow |V_r| < \frac{\lambda_0}{4T_r}$$

This is the unambiguous velocity limit.

**Example:** A target velocity inducing a phase shift  $\Delta\varphi = \pi + \varepsilon$  will be observed as a negative shift with  $\Delta\varphi = -\pi + \varepsilon$  to remain in the  $\pm \pi$  range.

This changes the sign and magnitude of the associated velocity  $\rightarrow$  **Folding**

# Pulse-pair processing

After each beam, at each range gate we get an amplitude and phase sample (phasor notation<sup>\*</sup>):

$$S_i = a_i + jb_i = A_i e^{j\varphi_i}$$

\*To recover the original sine wave:

$$s(t_i) = \operatorname{Re}\{S_i e^{j2\pi f_0 t_i}\} = A_i \cos(2\pi f_0 t_i + \varphi_i)$$

Integrating N pulses, we get for each gate:

Power (lag-0 autocorrelation) :

$$P = \frac{1}{N} \sum_{i=0}^{N-1} S_i S_i^* = \frac{1}{N} \sum_{i=0}^{N-1} A_i^2$$

Phase shift (lag-1 autocorrelation) :

$$\Delta\varphi = -\arg\left\{\frac{1}{N-1} \sum_{n=0}^{N-2} S_i S_{i+1}^*\right\} = -\arg\left\{\frac{1}{N-1} \sum_{n=0}^{N-2} A_i A_{i+1} e^{j(\varphi_i - \varphi_{i+1})}\right\}$$

Note: Doppler velocity resolution improves with the number of integrated pulses:

$$\Delta V_r = \frac{\lambda_0}{2NT_r}$$

# From DSD to Moments

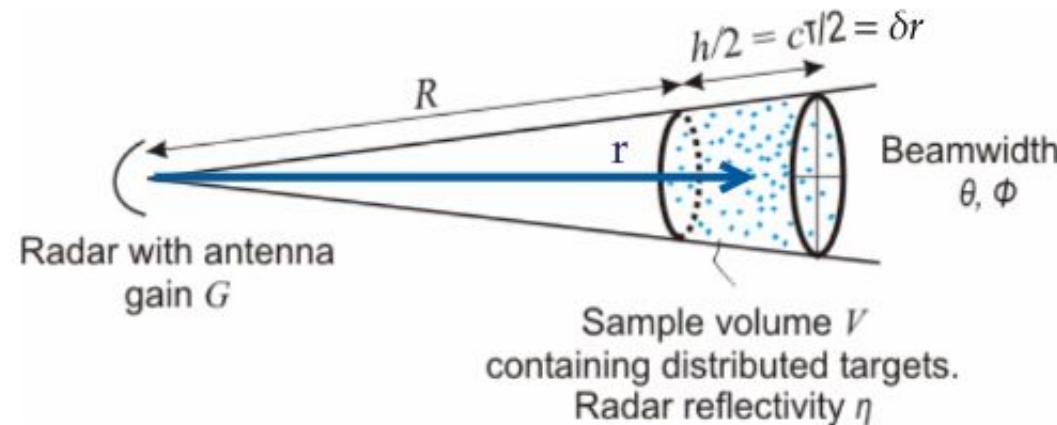
# Drop Size Distribution (DSD)

The radar samples a **volume** defined by a **beamwidth** and **“pulse” length**

A **radar measurement** integrates the **backscatter** of droplets within a **sampled volume** (e.g. thousands to millions !)

The backscatter signal is not from individual drops but from their statistical distribution

Knowing the **DSD allows to relate radar variables to cloud microphysics** (Liquid Water Content, rain rate, ...)

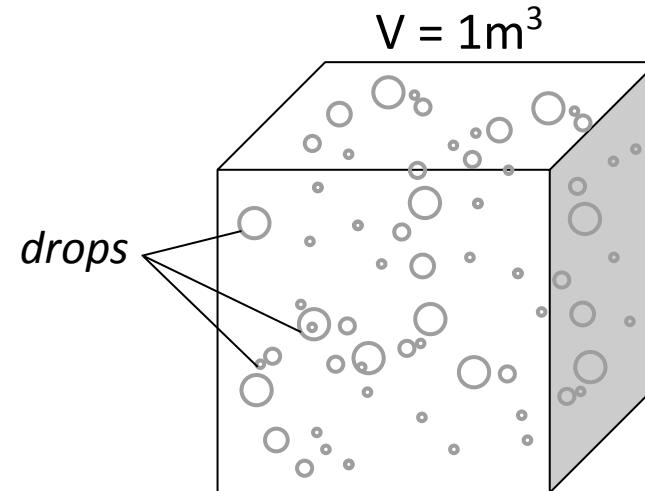


# Drop Size Distribution (DSD)

**DSD:**  $N(D)$ , number, per unit of volume, of drops for which size is between  $D$  and  $D+dD$

$$N(D) = N_0 e^{-\lambda D} \text{ [m}^{-3} \text{.mm}^{-1}\text{]} \text{ (Marshall-Palmer)}$$

The total number of drops, per unit of volume,  $N_t$  is:



$$N_t = \int_{D_{\min}}^{D_{\max}} N(D) dD$$



# Moments of the DSD

The **DSD** is described by its **moments**:

$$M_n = \int N(D) \cdot D^n dD$$

Order n	Moment $M_n$	Physical meaning	Units
0	$M_0$	Total number of drops	$m^{-3}$
1	$M_1$	Mean Drops size	$mm \cdot m^{-3}$
2	$M_2$	Extinction coeff (optical)	$mm^2 \cdot m^{-3}$
3	$M_3$	Liquid Water Content (LWC)	$mm^3 \cdot m^{-3}$
6	$M_6$	Reflectivity factor (Z)	$mm^6 \cdot m^{-3}$

## Instrument and their sensitivity to DSD moments:

- Radar → reflectivity  $Z$  ( $mm^6 \cdot m^{-3}$ ) →  $M_6$
- Raingauge → rainfall rate  $R$  ( $mm \cdot h^{-1}$ ) →  $M_3 \cdot 67$  (Marshall-Palmer)
- Microwave radiometer →  $\propto M_3$  (LWP)
- Lidar →  $M_0$  &  $M_2$  ( $\alpha$ )

# Importance of knowing dropsizes

- Radar reflectivity  $Z \propto D^6$  → a few **large drops** can **dominate Z**
- **Water volume  $\propto D^3$**  → doesn't grow as fast as Z with drop size

Drop Size	Concentration [ $\# \cdot m^{-3}$ ]	Reflectivity Z	Water volume per cubic meter
1 mm	4096	36 dBZ	2144.6 mm <sup>3</sup>
4 mm	1	36 dBZ	33.5 mm <sup>3</sup>

**Radar reflectivity is highly sensitive to large drops**

Two clouds can have the same Z but very different water content

→ **Be cautious when using Z to estimate liquid water content!**

**Tomorrow**

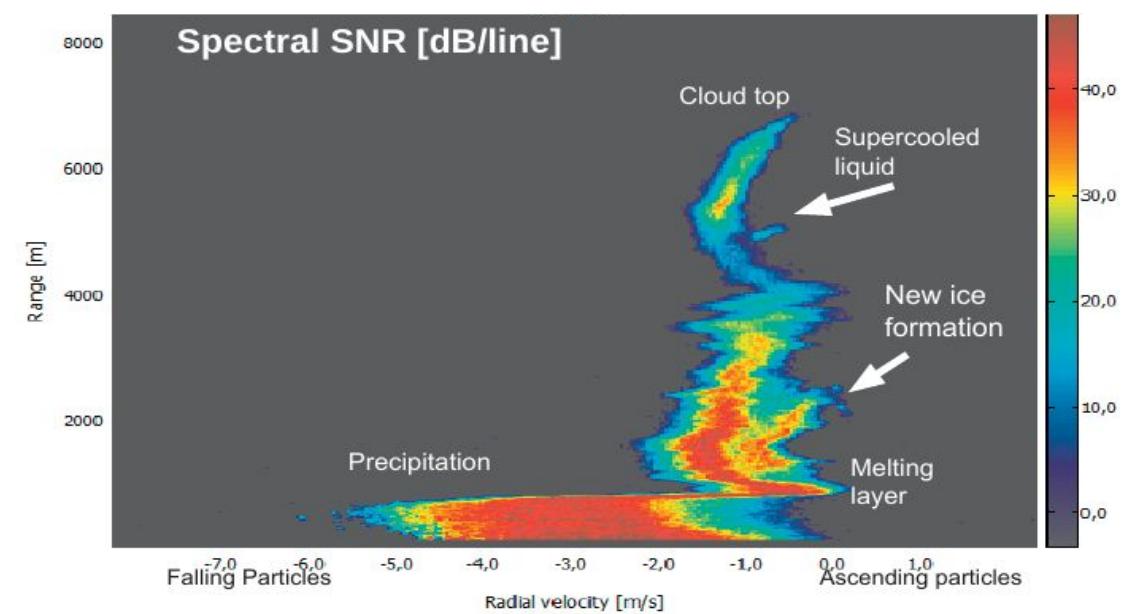
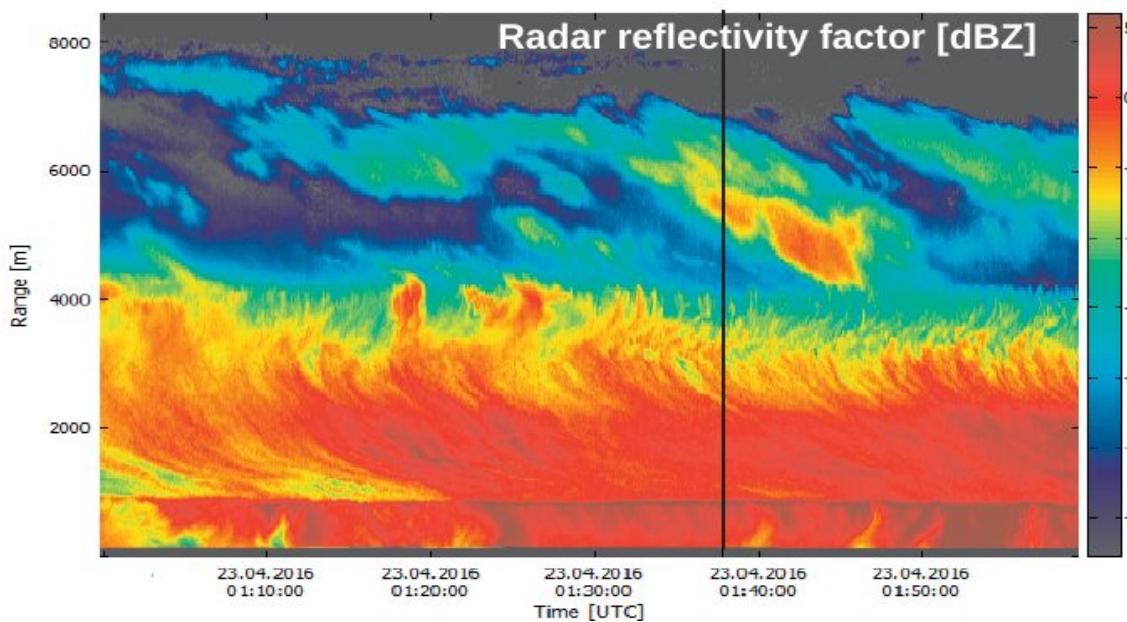
Lecture : Visualization and interpretation of radar doppler spectra 9:00 - 10:30, S. Kneifel (LMU)

Hands-on : Cloud radar doppler spectra analysis with peako and peaktree, 14:00 - 17:30, M. Radenz (TROPOS)

# Doppler Spectra

# Doppler Spectra

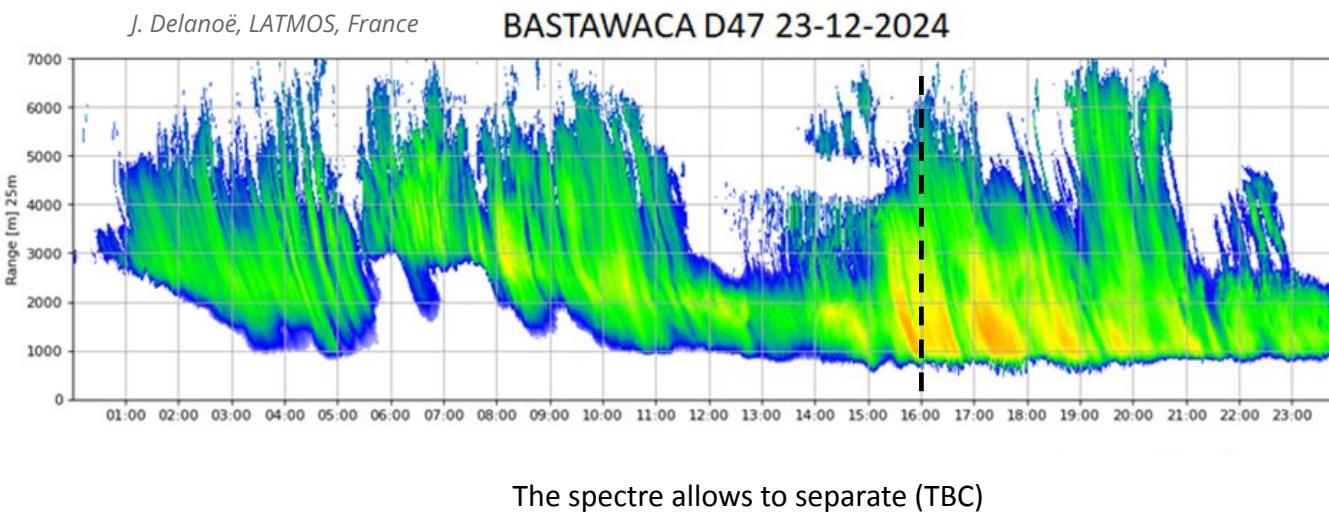
- Doppler spectra provide **more information** than just mean velocity: they show the **full distribution of particle fall speeds** in the **radar sampling volume**.
- Because **larger particles** typically **fall faster**, the **Doppler spectrum** helps to infer the **Particle Size Distribution (PSD)**.
- This is especially **useful** for **micropysical retrievals**, such as **distinguishing** between **cloud droplets, raindrops, or snowflakes**.



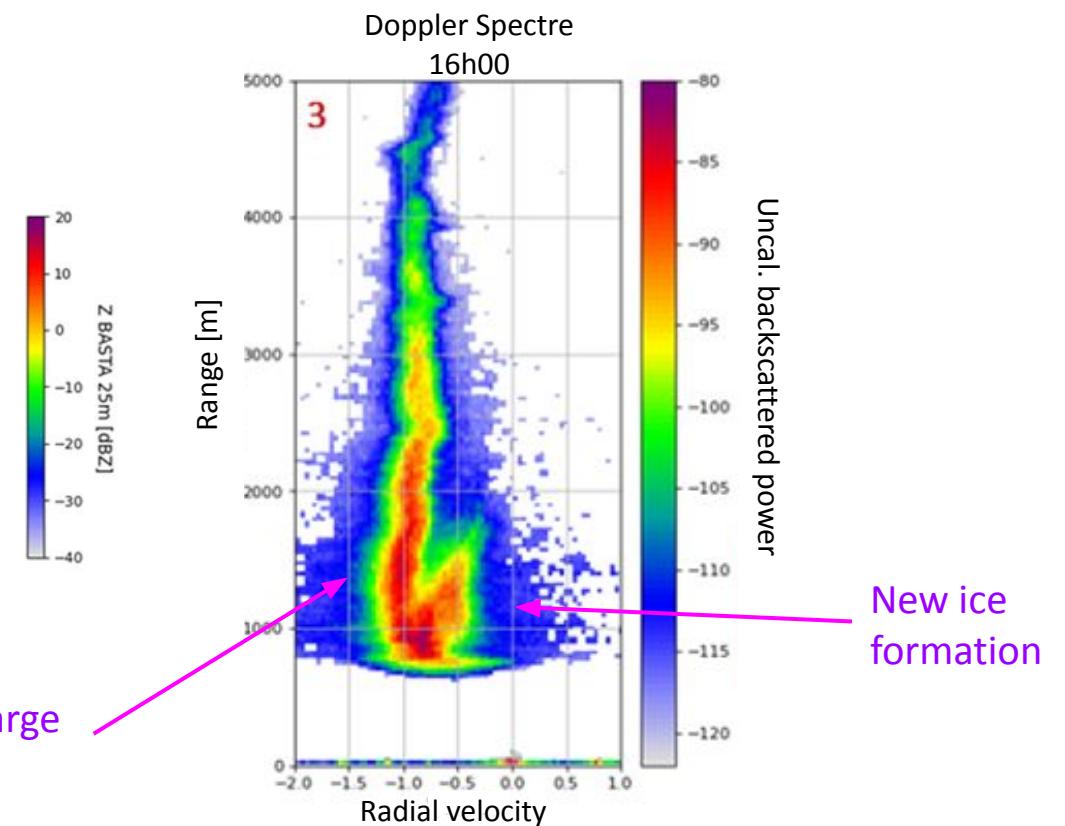
From RPG documentation, sept 2017

# Doppler Spectra

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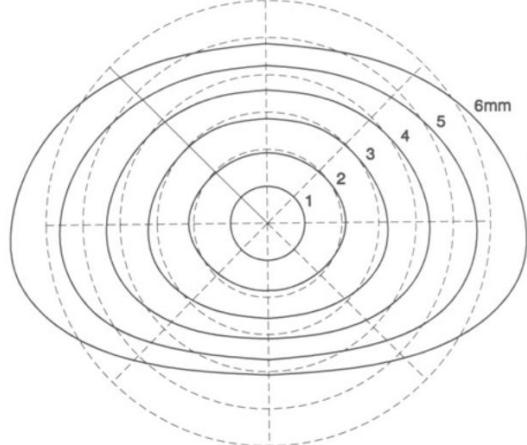
Descending large  
ice particles



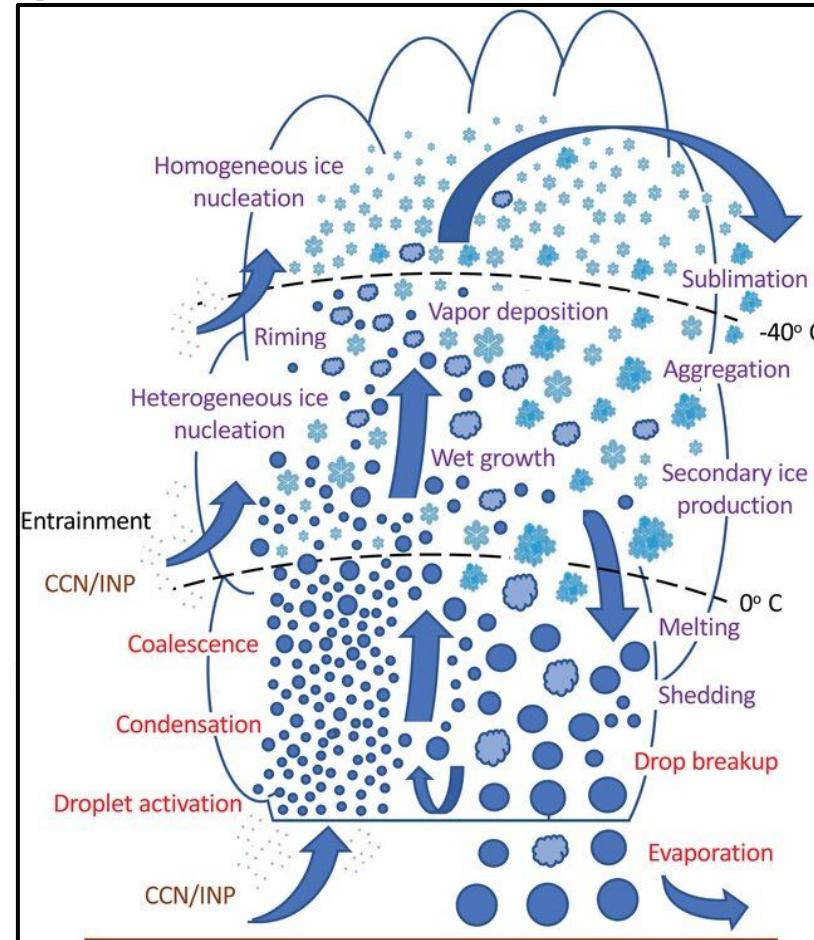
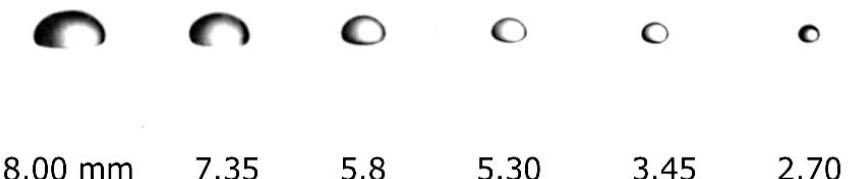
# Polarimetry

# Can polarimetry add information ?

Yes, because **hydrometeors are not spheres**



From Beard and Chuang, 1987

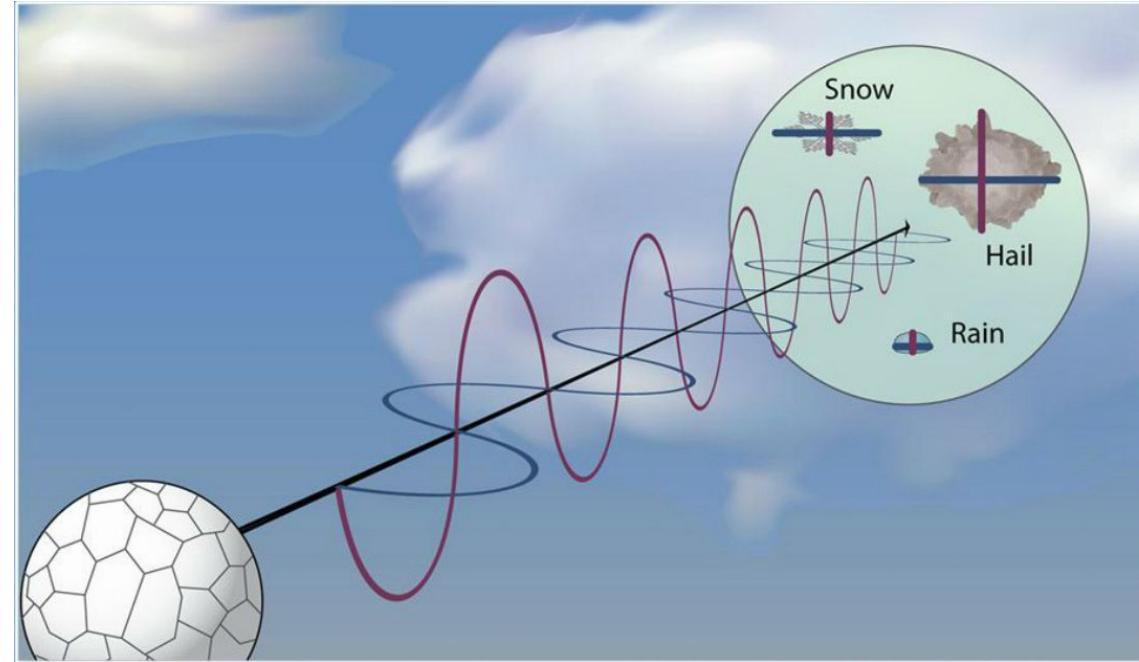
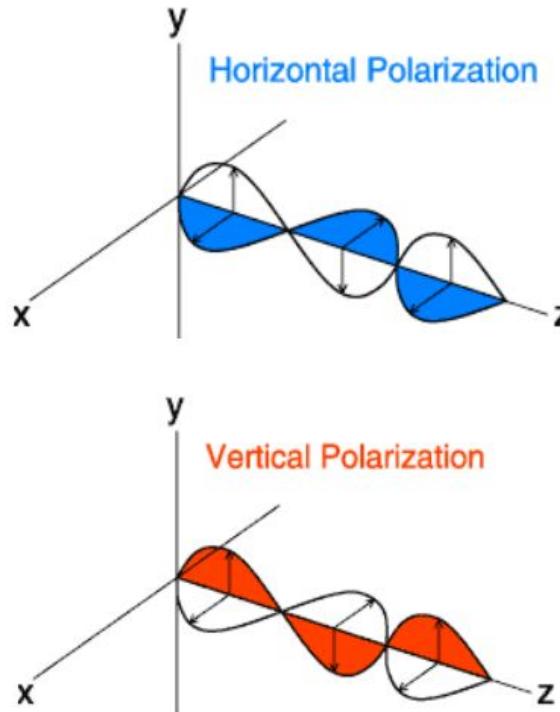


<https://doi.org/10.1029/2019MS001689>



# Dual polarization principles

When the **particle** becomes **oblate** or **prolate**, the backscattering becomes **polarization dependent**



*Credit: National Weather Service*

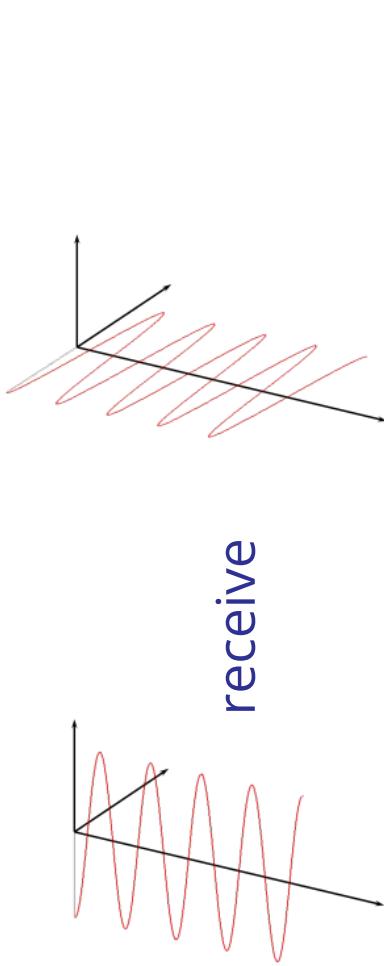
**Also improves** clutter removal, melting layer detection, lightning activity identification, and hail detection, ...

# Polarimetric operation modes and their implications

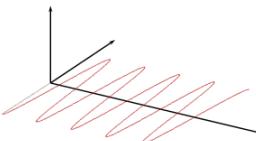
1. **STAR Mode — Simultaneous Transmit and Receive (e.g. Météo-France weather radar)**
  - a. Transmit simultaneously in H and V (co-polar).
  - b. Receive simultaneously in H and V.
  - c. Measures:  $Z_{DR}$ ,  $\rho_{HV}$ ,  $\Phi_{DP}$ ,  $K_{DP}$ .
  - d. Advantage: fast, no switching needed (good time resolution).
  - e. Limitation: does not provide pure cross-pol (no LDR or HV→VH).
2. **Alternating H/V Mode (Pulse Switching)**
  - a. Transmit alternately H and V pulses.
  - b. Receive in same polarization as transmit pulse (H→H, V→V).
  - c. Good estimates of  $Z_{DR}$ ,  $\rho_{HV}$ , sometimes LDR.
  - d. Common in precipitation radars (e.g. USA NEXRAD).
3. **Cross-Polar/LDR Mode**
  - a. Transmit in H (or V), receive in orthogonal polarization (V or H).
  - b. Allows measurement of LDR and cross-polar correlation.
  - c. Requires dedicated or sequential setup.
  - d. Typical for **cloud radars**, to study depolarization and phase.

Access to **DPOL variables** depends on the chosen **polarimetric mode**.

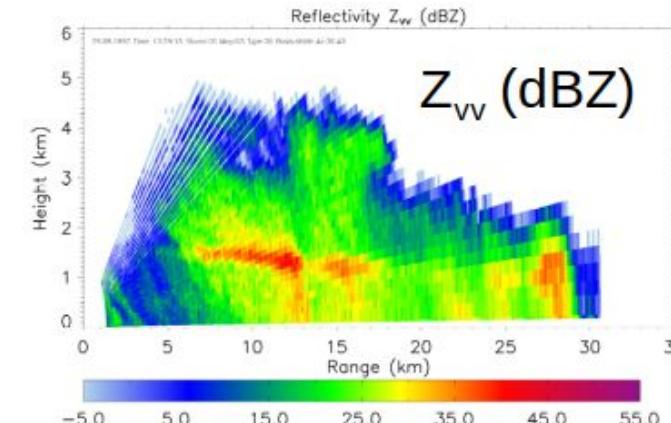
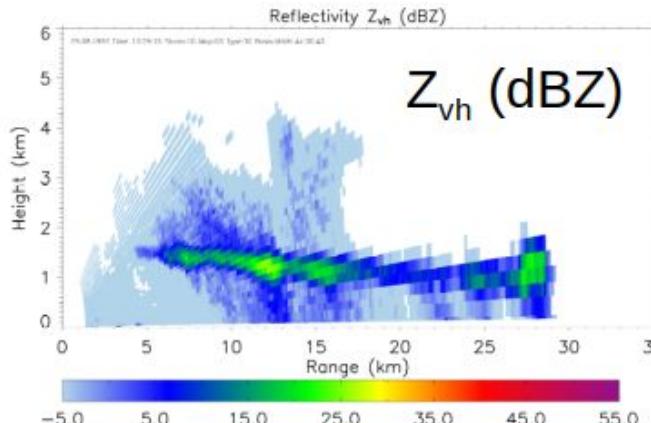
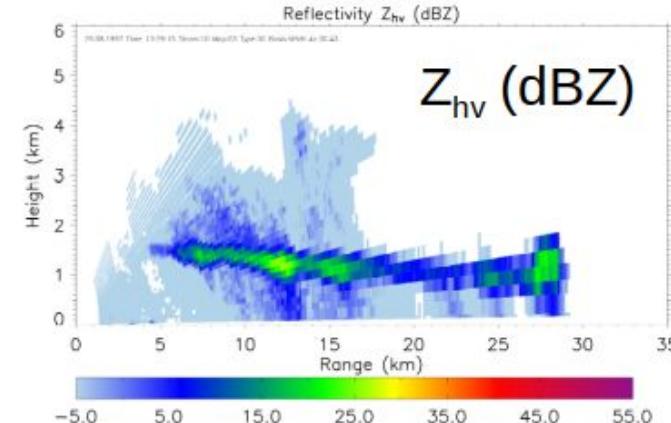
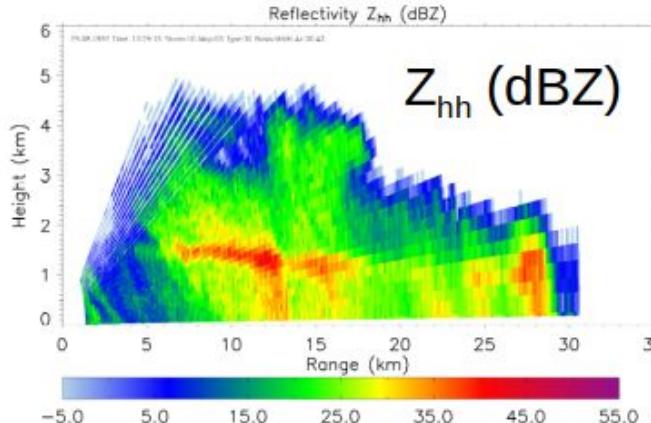
# DPOL observations



receive



transmit



NB: capability here to receive the co- and cross-polar component

From H. Russchenberg, TU Delft Master lesson on cloud radar 2015  
 Data: POLDIRAD (DLR, Oberpfaffenhofen, Germany), Prof. Madhu Chandra

# Dual Polarization variables : STAR mode

## $Z_{DR}$ : Differential reflectivity [dB]

- $Z_{DR} = Z_H - Z_V$  [dB]
- Indicates particle shape/orientation (oblate raindrops vs spherical ice crystals)

## $\Phi_{DP}$ : Differential Phase [°]

- $\Phi_{DP} = \phi_H - \phi_V$  [°]
- Sensitive to particle shape and concentration. Useful for identifying liquid water content and melting layers

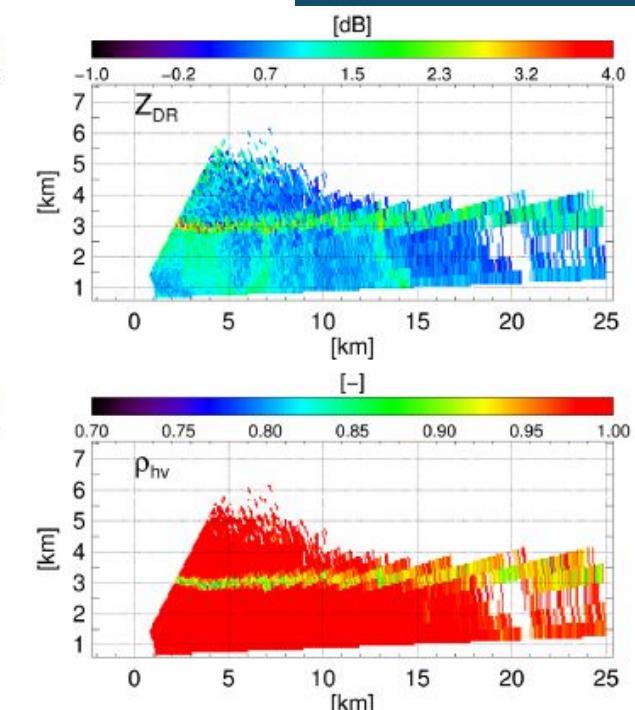
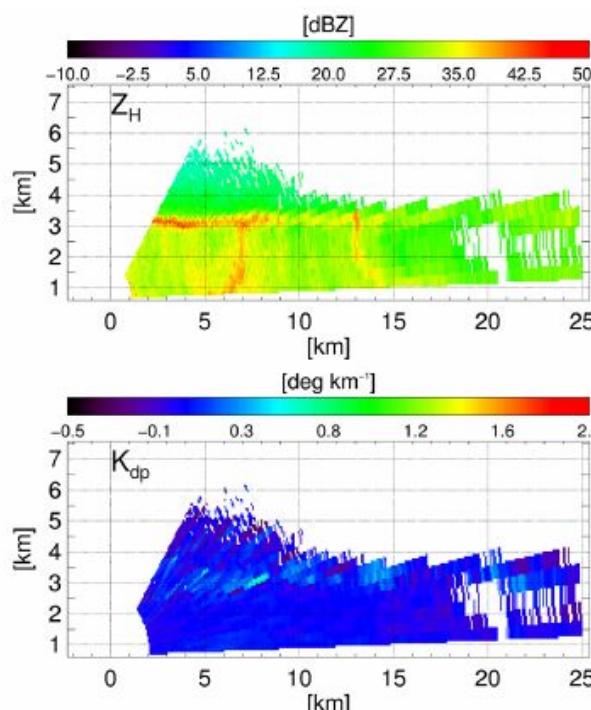
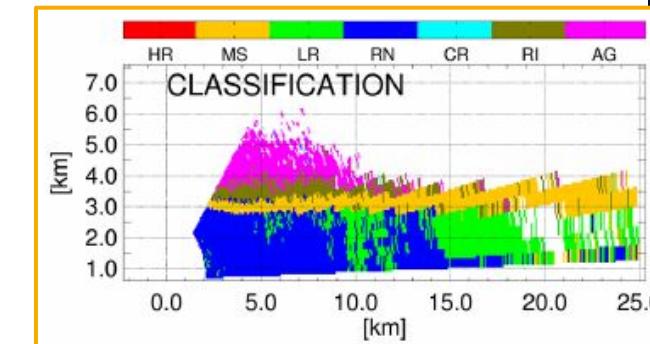
## $K_{DP}$ : Specific differential phase [ $^{\circ} \cdot \text{km}^{-1}$ ]

$$K_{DP} = \int_r^{r+\delta r} \left( \frac{d\Phi_{DP}}{dr} \right) [^{\circ} \cdot \text{km}^{-1}]$$

- Independent of radar calibration
- ~ unaffected by attenuation/blocking

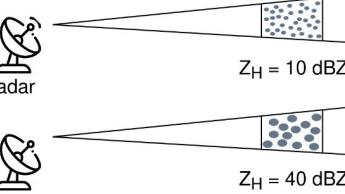
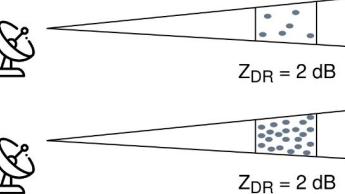
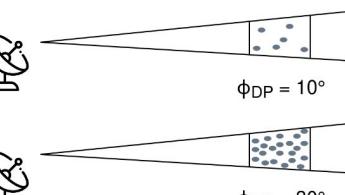
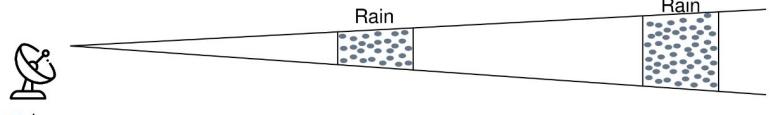
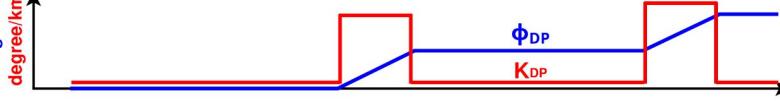
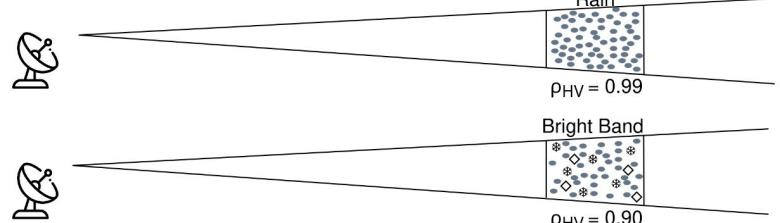
## $\rho_{HV}$ : Correlation coefficient [-]

- Cross-correlation between horizontally/vertically polarized returned signals
- Measures similarity between the 2 polarization channels.
- High values indicate uniform particle type/shape
- Useful for detecting melting layer, hail



From Grazioli et al., 2015  
X-band DPOL radar

# Dual Polarization variables: STAR mode

	Effect of hydrometeor <b>shape</b>	Effect of hydrometeor <b>concentration</b>
<b><math>Z_H</math></b> Horizontal Reflectivity	 $Z_H = X$ (dBZ) $Z_H > X$ $Z_H < X$	 $Z_H = 10$ dBZ $Z_H = 40$ dBZ
<b><math>Z_{DR}</math></b> Differential Reflectivity	 $Z_{DR} = 0$ (dB) $Z_{DR} > 0$ dB $Z_{DR} < 0$ dB	 $Z_{DR} = 2$ dB $Z_{DR} = 2$ dB
<b><math>\phi_{DP}</math></b> Differential Phase	 $\phi_{DP} = 0^\circ$ $\phi_{DP} > 0^\circ$ $\phi_{DP} < 0^\circ$	 $\phi_{DP} = 10^\circ$ $\phi_{DP} = 30^\circ$
<b><math>K_{DP}</math></b> Specific Differential Phase		 
<b><math>\rho_{HV}</math></b> Correlation Coefficient		

# Dual Polarization variables: cross-polar mode

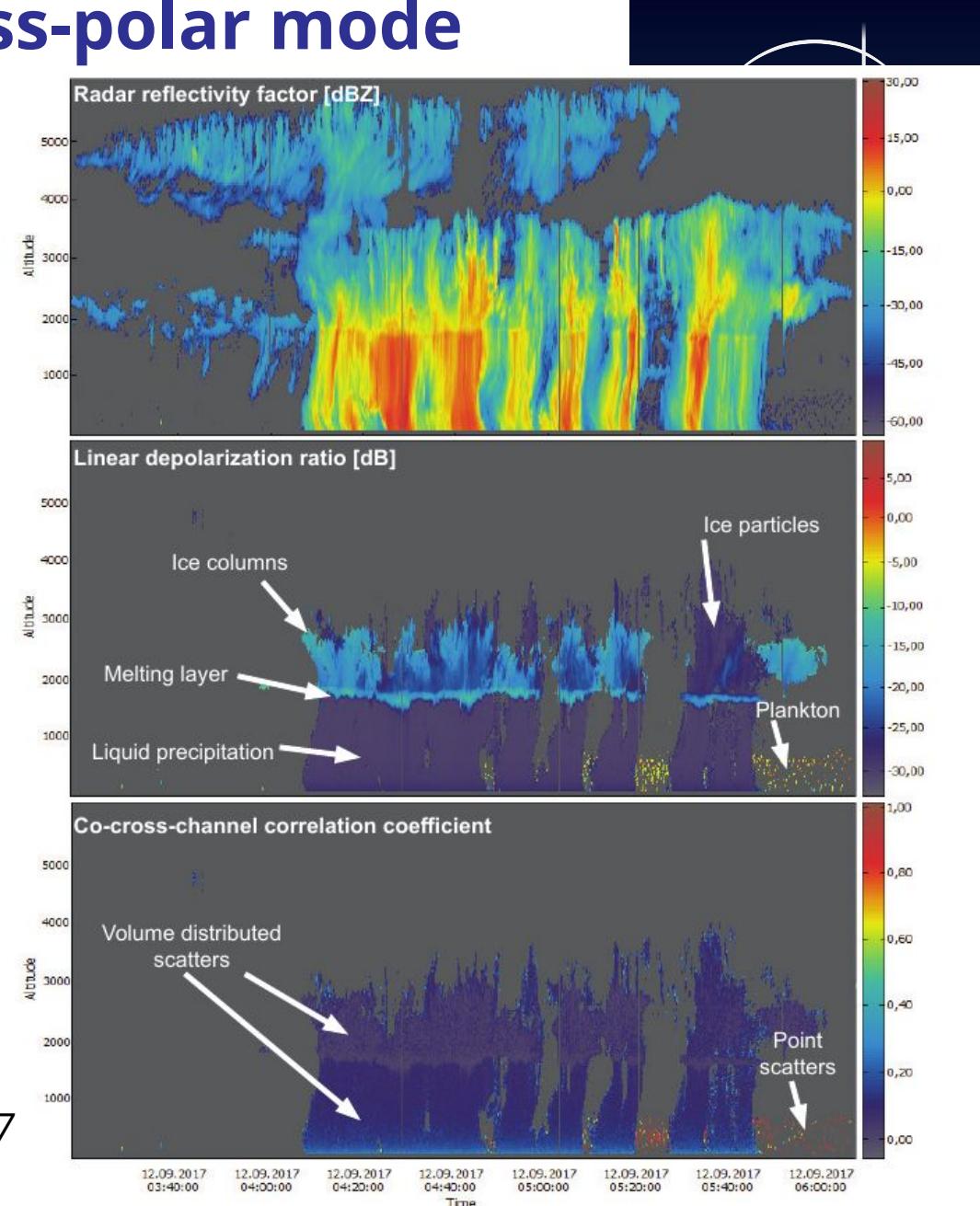
## LDR: Linear Depolarization Ratio [dB]

- Ratio of cross-polarized power to co-polarized power (typically horizontal transmission and vertical reception)
- Indicates particle shape irregularities, nonsphericity, and orientation diversity

## Co-Cross Channel Correlation Coefficient [-]

- Correlation between co-polarized and cross-polarized channels
- Provides additional discrimination of particle types and helps identify complex scattering mechanism
- Usually low values [0.4-0.8]

*From RPG documentation, sept 2017*



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Thank you !